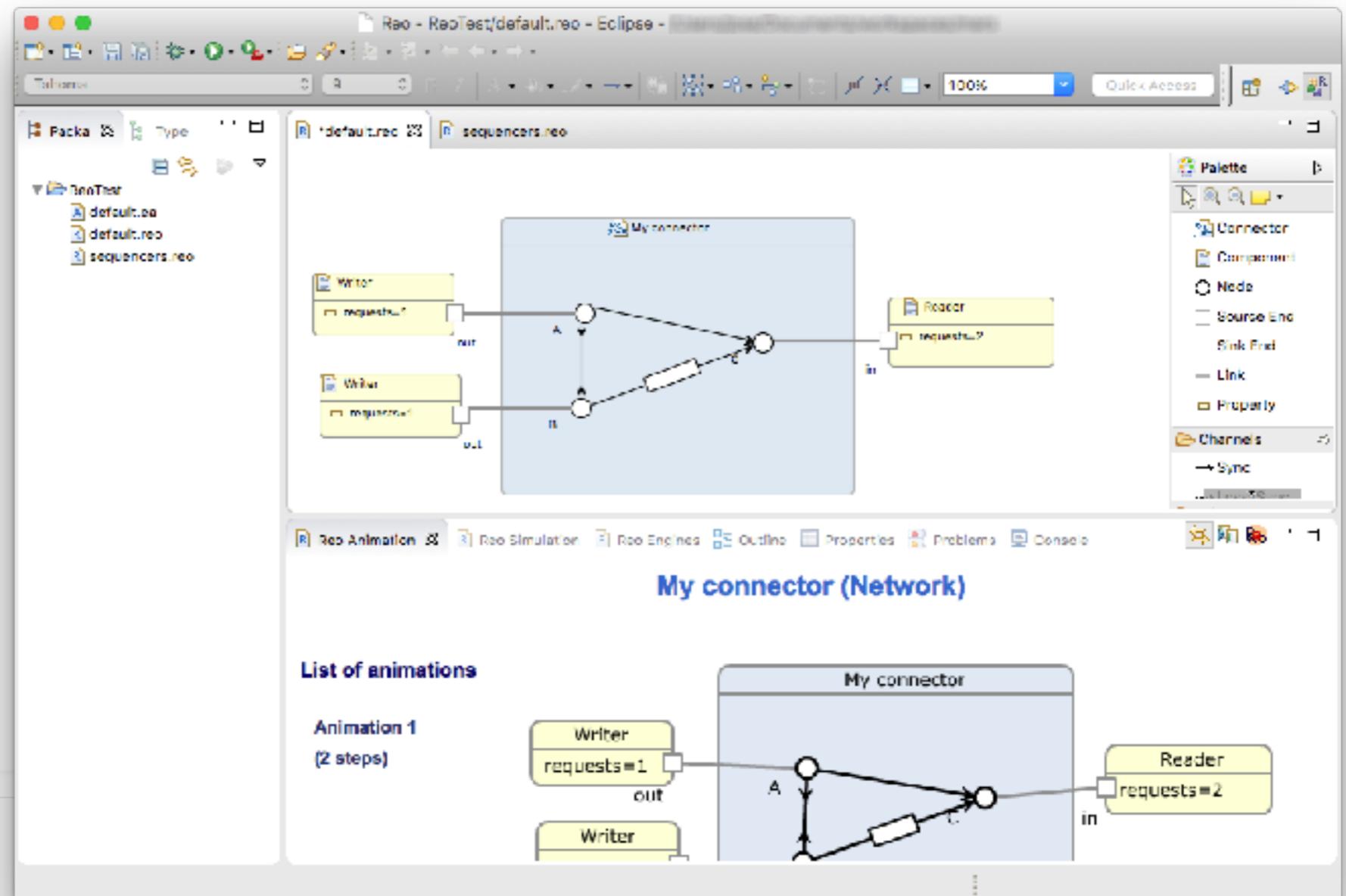


Architectural design: the coordination perspective

José Proença & Luís Soares Barbosa
HASLab - INESC TEC & UM
Arquitectura e Cálculo 2017-18



Reo eclipse toolset



get Eclipse

update site: <http://reo.project.cwi.nl/update>

Reo Live

Reo Live Families About

Input (Shift-Enter to update)
merger ; lossy ; fifo

Type
2 -> 1

Concrete instance
merger ; (lossy ; fifo): 2 -> 1

examples
writer reader fifo
merger dupl drain

Circuit of the instance

Automaton of the instance (under development)

mCRL2 of the instance

JavaScript: <https://reolanguage.github.io/ReoLive/snapshot/>

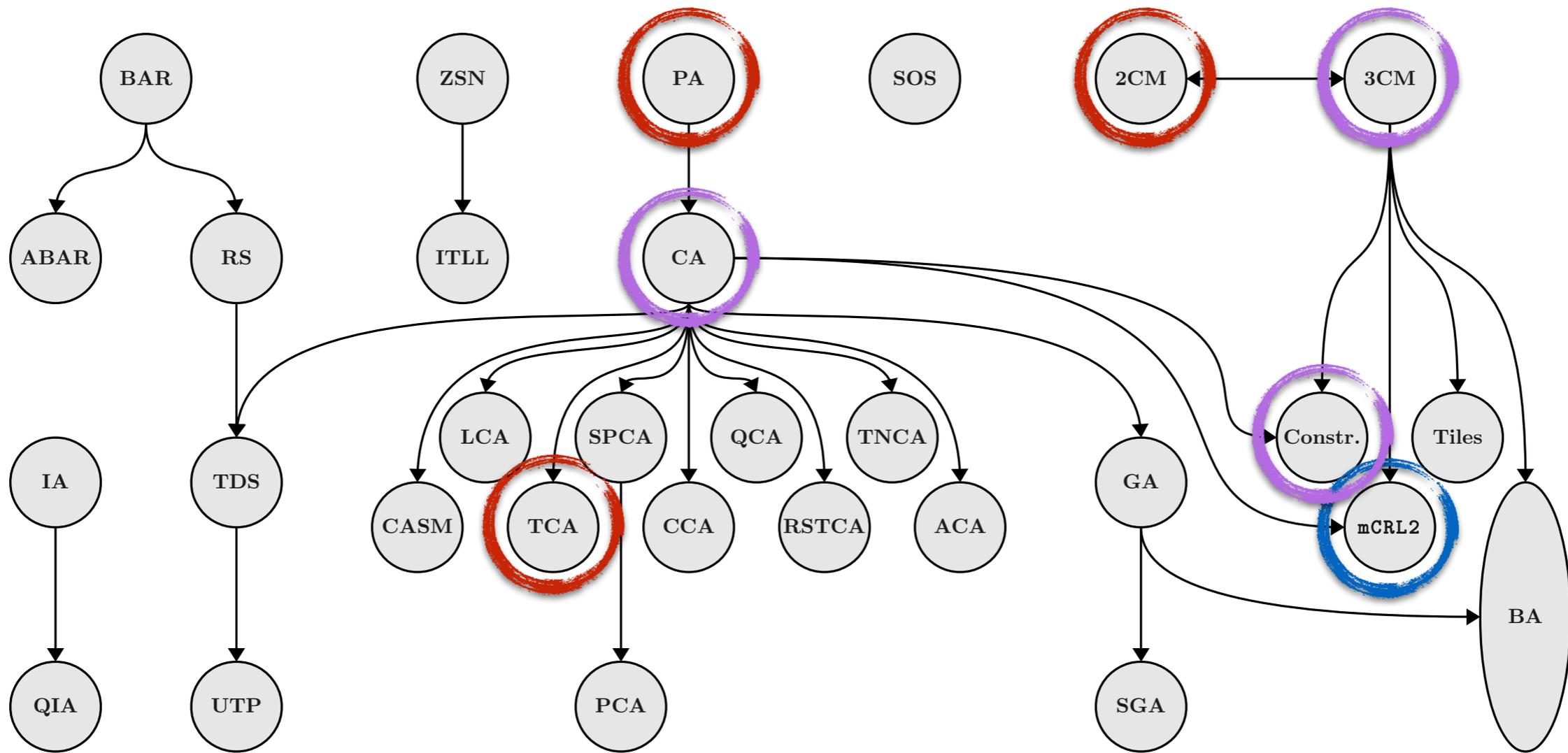
Reo semantics

Jongmans and Arbab 2012

Overview of Thirty Semantic Formalisms for Reo

Reo semantics

- *Coalgebraic models*
 - Timed data streams
 - Record streams
- *Coloring models*
 - **Two colors**
 - **Three colors**
 - Tile models
- *Other models*
 - **Process algebra**
 - **Constraints**
 - Petri nets & intuitionistic logic
 - Unifying theories of programming
 - Structural operational semantics
- *Operational models*
 - **Constraint automata**
 - Variants of constraint automata
 - **Port automata**
 - **Timed**
 - Probabilistic
 - Continuous-time
 - Quantitative
 - Resource-sensitive timed
 - Transactional
 - Context-sensitive automata
 - Büchi automata
 - Reo automata
 - Intentional automata
 - Action constraint automata
 - Behavioral automata
 - Structural operational semantics



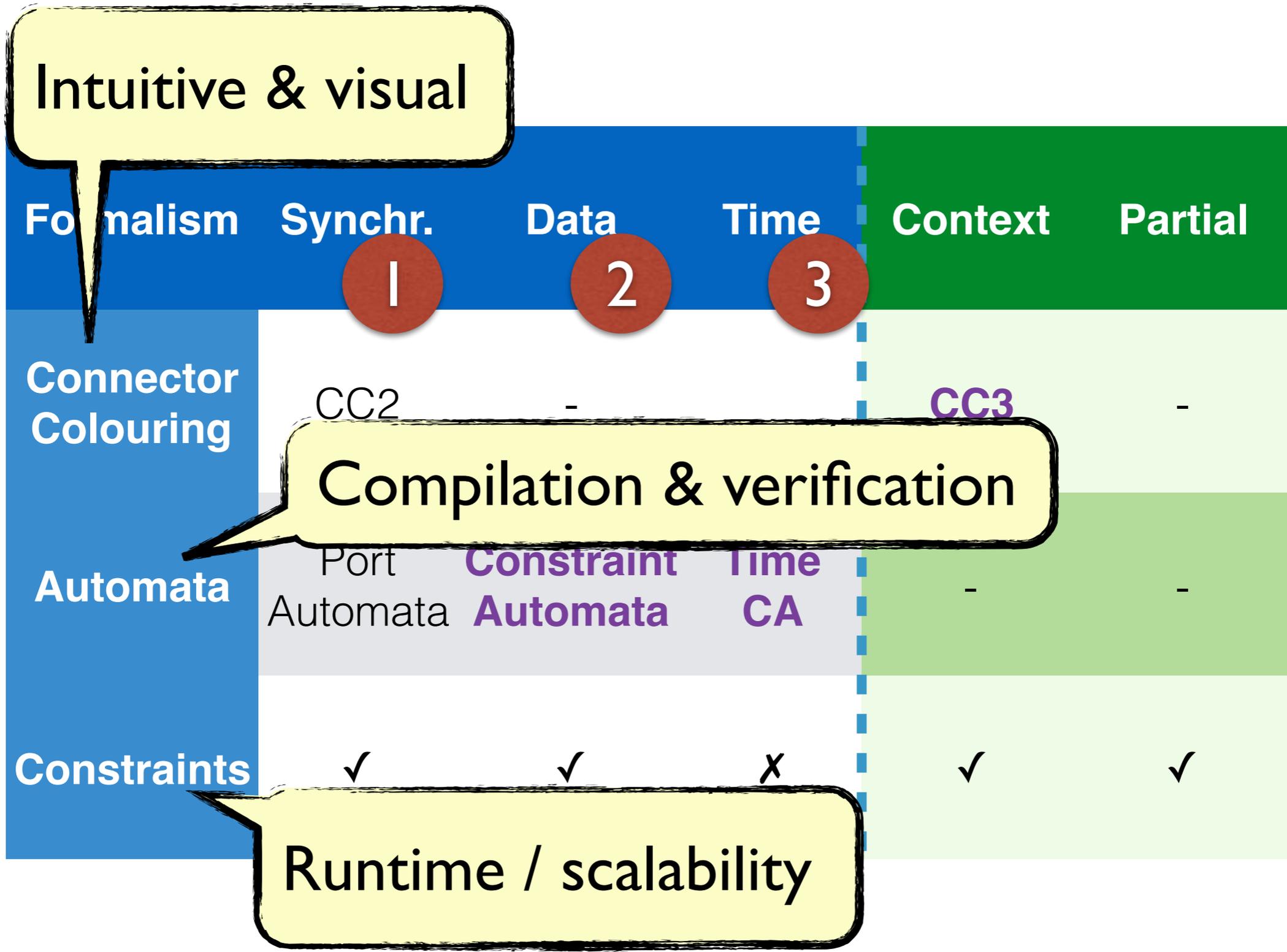
2CM : Coloring models with two colors [28, 29, 33]
 3CM : Coloring models with three colors [28, 29, 33]
 ABAR : Augmented BAR [39, 40]
 ACA : Action CA [46]
 BA : Behavioral automata [61]
 BAR : Büchi automata of records [38, 40]
 CA : Constraint automata [10, 17]
 CASM : CA with state memory [60]
 CCA : Continuous-time CA [18]
 Constr.: Propositional constraints [30, 31, 32]
 GA : Guarded automata [20, 21]
 IA : Intentional automata [33]
 ITLL : Intuitionistic temporal linear logic [27]
 LCA : Labeled CA [44]
 mCRL2 : Process algebra [47, 48, 49]

PA : Port automata [45]
 PCA : Probabilistic CA [15]
 QCA : Quantitative CA [12, 53]
 QIA : Quantitative IA [13]
 RS : Record streams [38, 40]
 RSTCA : Resource-sensitive timed CA [51]
 SGA : Stochastic GA [56, 57]
 SOS : Structural operational semantics [58]
 SPCA : Simple PCA [15]
 TCA : Timed CA [8, 9]
 TDS : Timed data streams [4, 5, 14, 62]
 Tiles : Tile models [11]
 TNCA : Transactional CA [54]
 UTP : Unifying theories of programming [55, 52]
 ZSN : Zero-safe nets [27]

Outline

Formalism	Synchr.	Data	Time	Context	Partial
Connector Colouring	CC2	-		CC3	-
Automata	Port Automata	Constraint Automata	Time CA	-	-
Constraints	✓	✓	✗	✓	✓

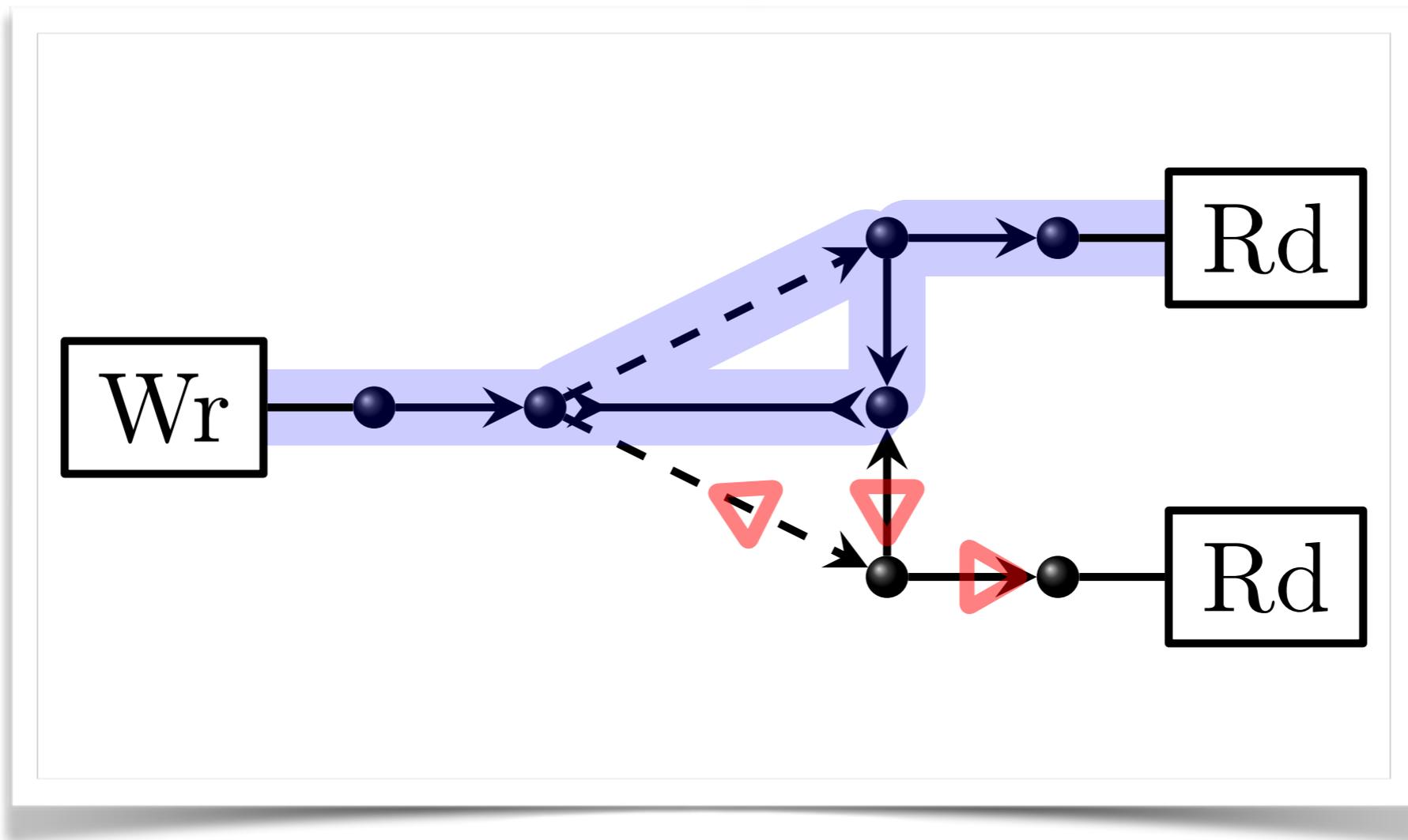
Outline



Intuitive & visual

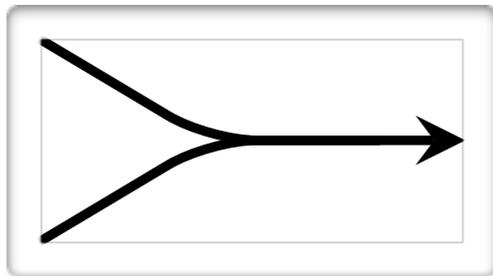
Compilation & verification

Runtime / scalability



Reo Connector Colouring

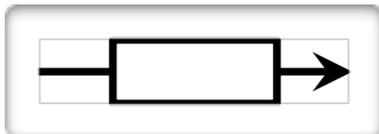
Behaviour?



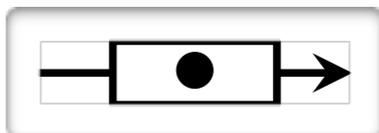
merger: data flows from one of the source ends to the sink end



lossy-sync: either data flows from the source to the sink end, OR it is lost

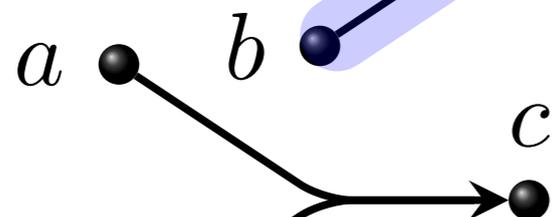
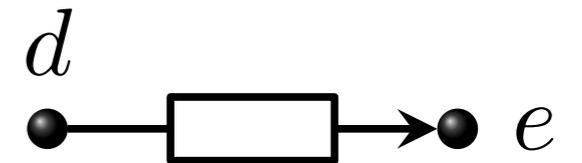
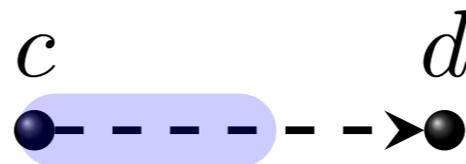
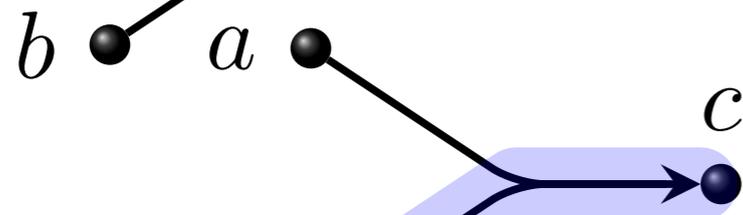
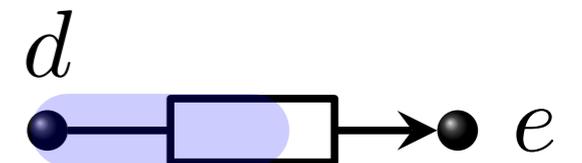
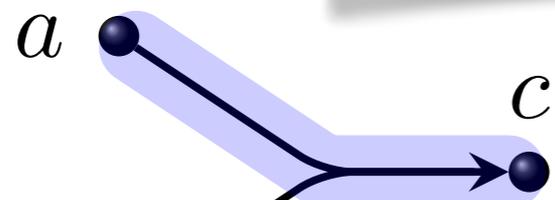
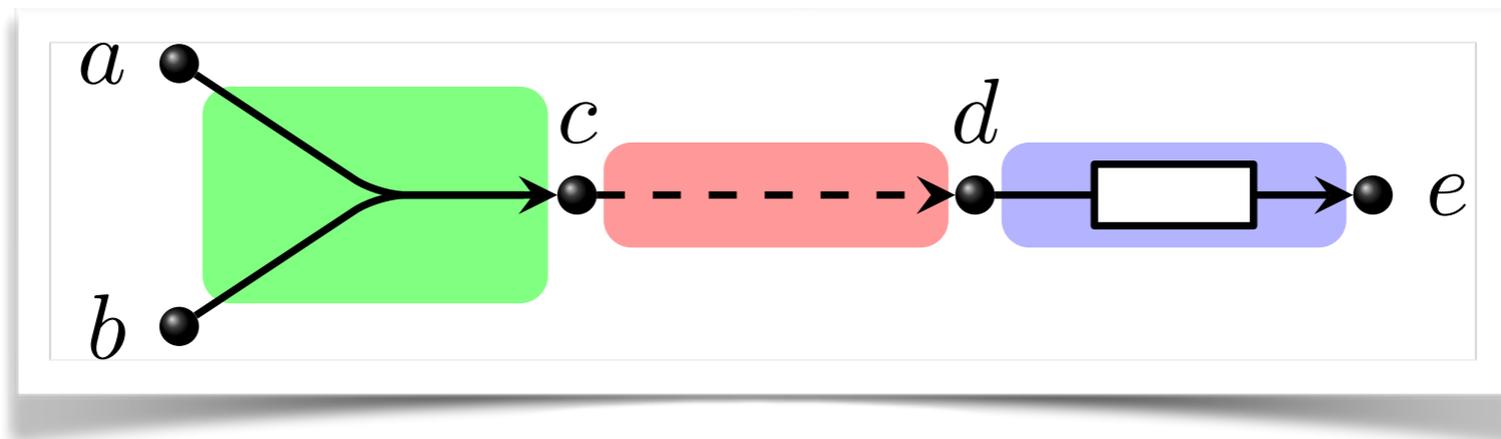


FIFO-1: data flows from the source end to the buffer, becoming a **FIFOFull-1**

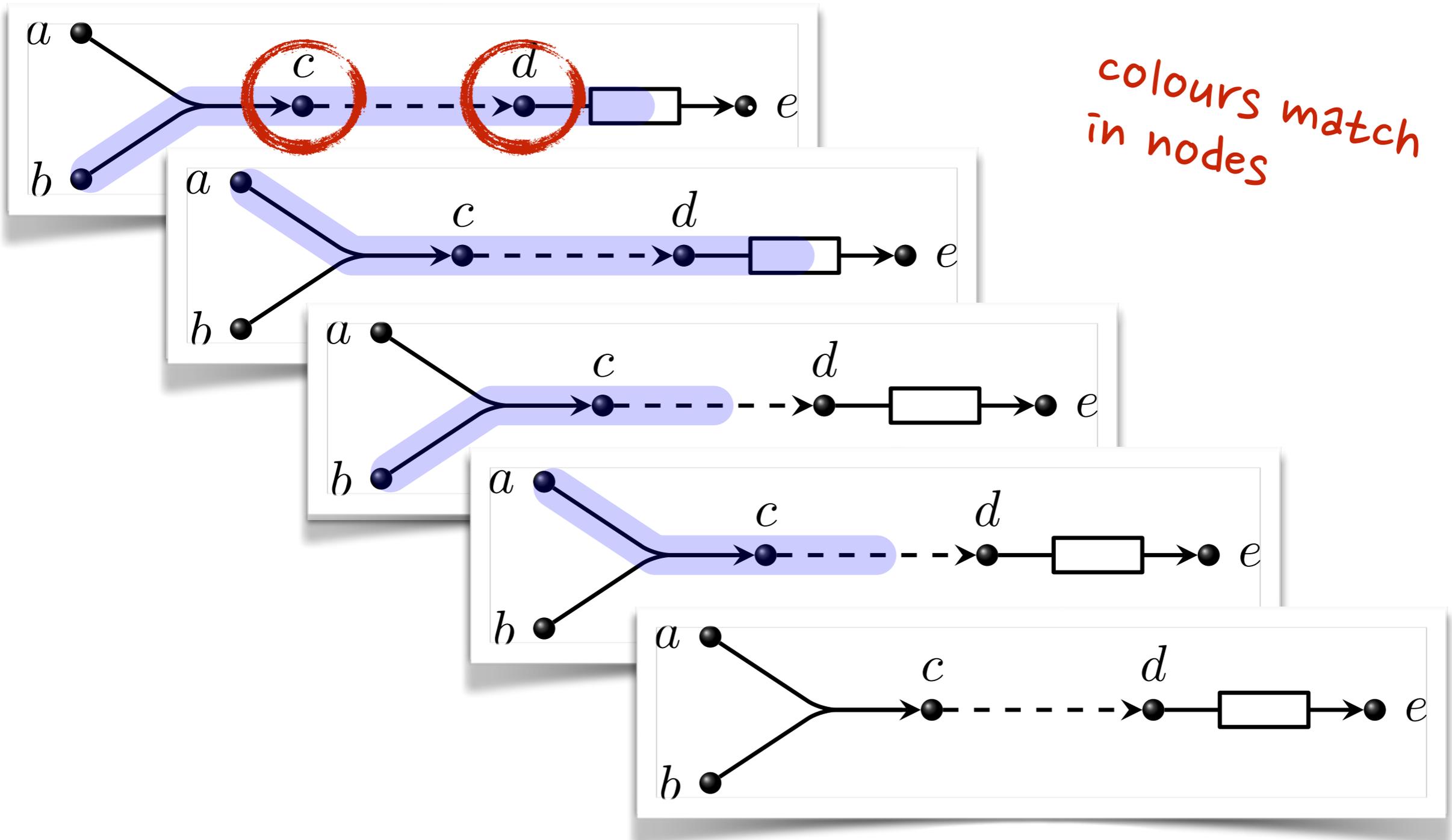


FIFOFull-1: data flows from the buffer to the sink buffer, becoming a **FIFO-1**

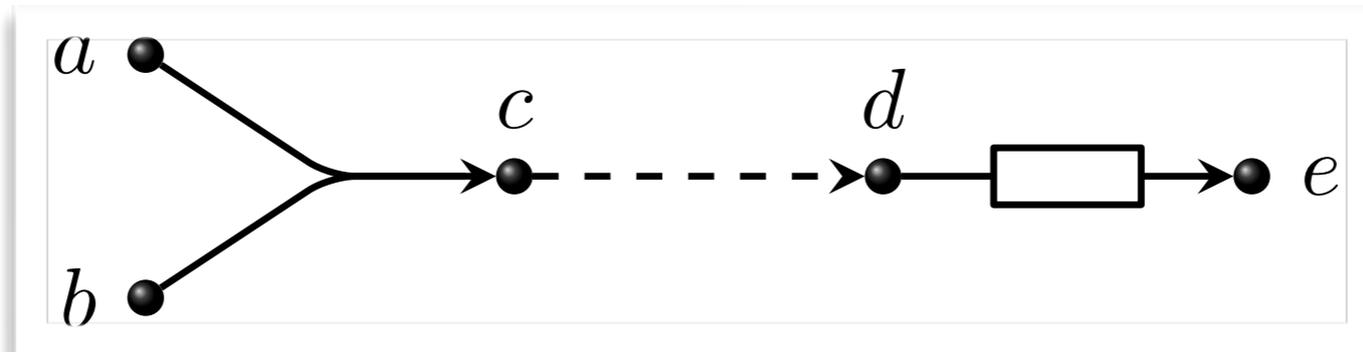
Colourings to describe synchronous dataflow



Colouring composition



Possible behaviour



1, 2, 3, ...

4, 5, 6, ...

1, 2, 3, ...

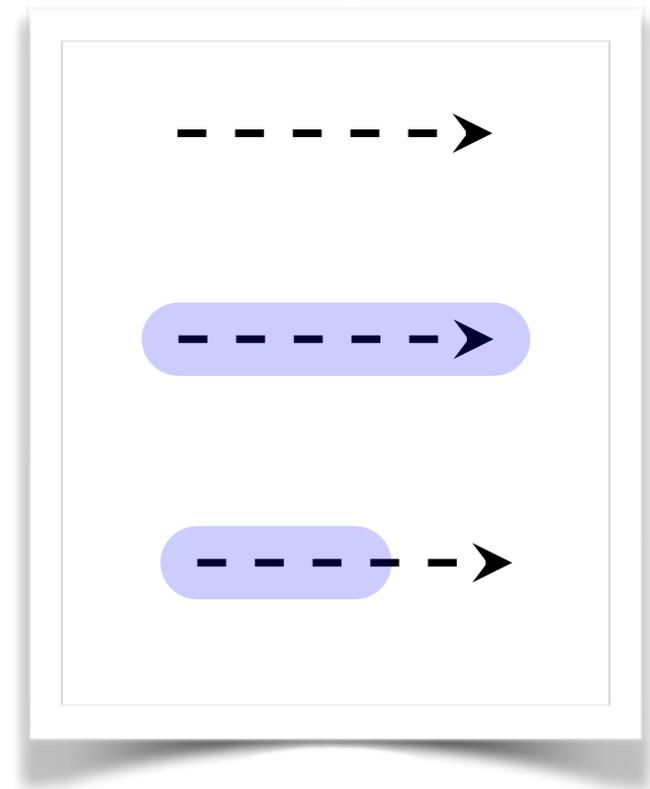
4, 5, 6, ...

1, 4, 6, 3, ...

1, 2, 3, 4, 5, 6, ...

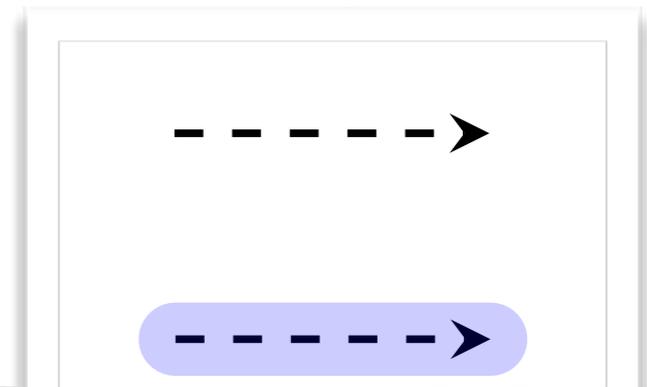
Colouring semantics (CC2)

- *Colouring*: End \rightarrow {Flow, NoFlow}
- *Colouring table*: Set(Colouring)
- *Composition* = matching colours
- More visual (intuitive)
- Used for generating animations



Colouring semantics (CC2)

- *Colouring*: End \rightarrow {Flow, NoFlow}
- *Colouring table*: Set(Colouring)
- *Composition* = matching colours



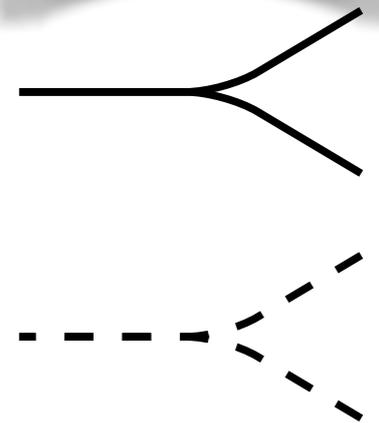
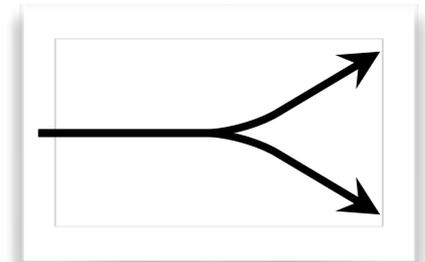
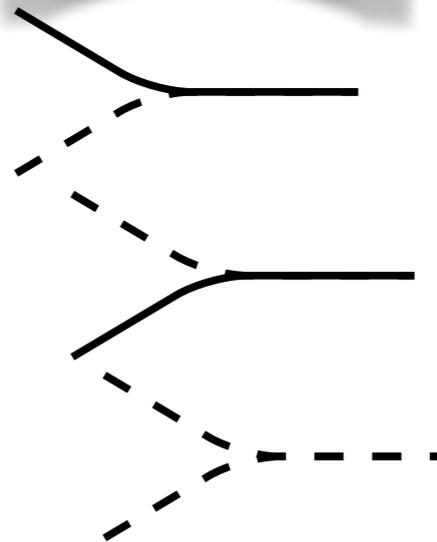
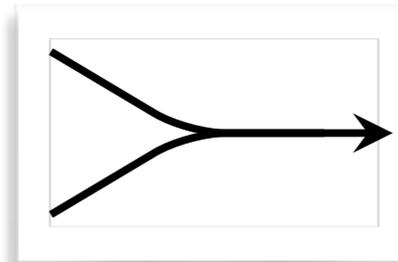
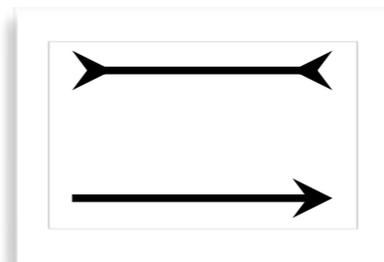
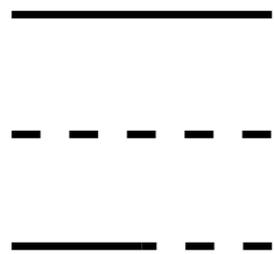
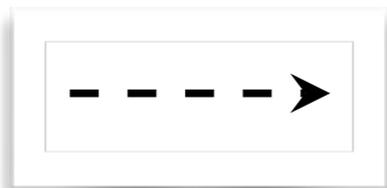
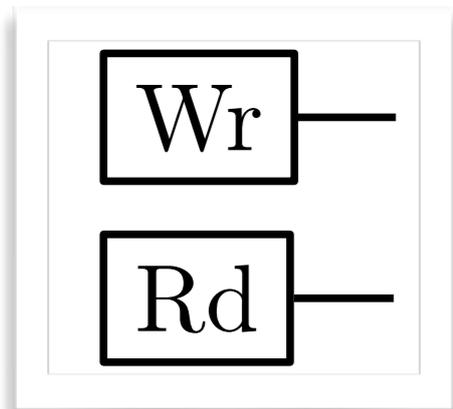
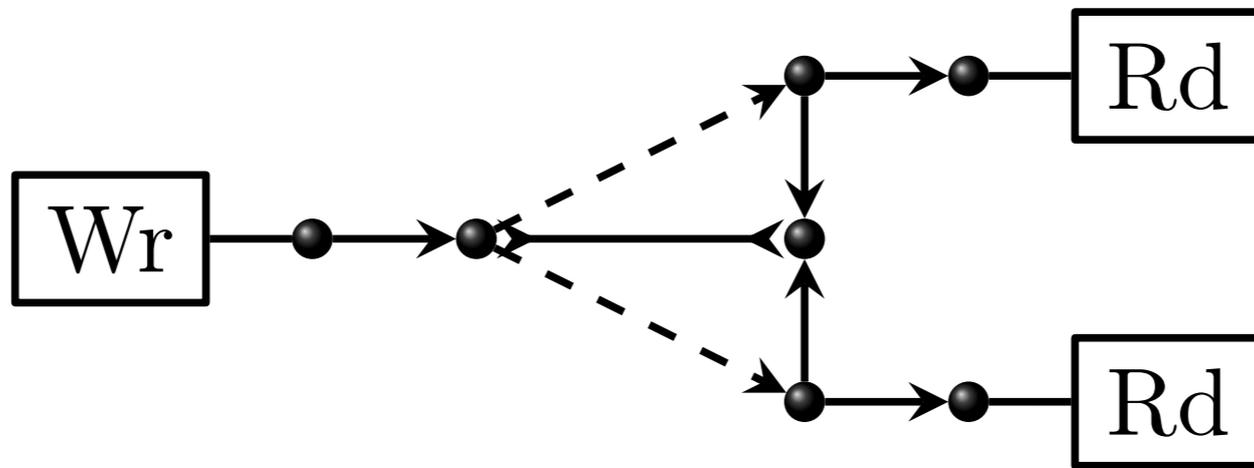
$$CT_1 \bowtie CT_2 =$$

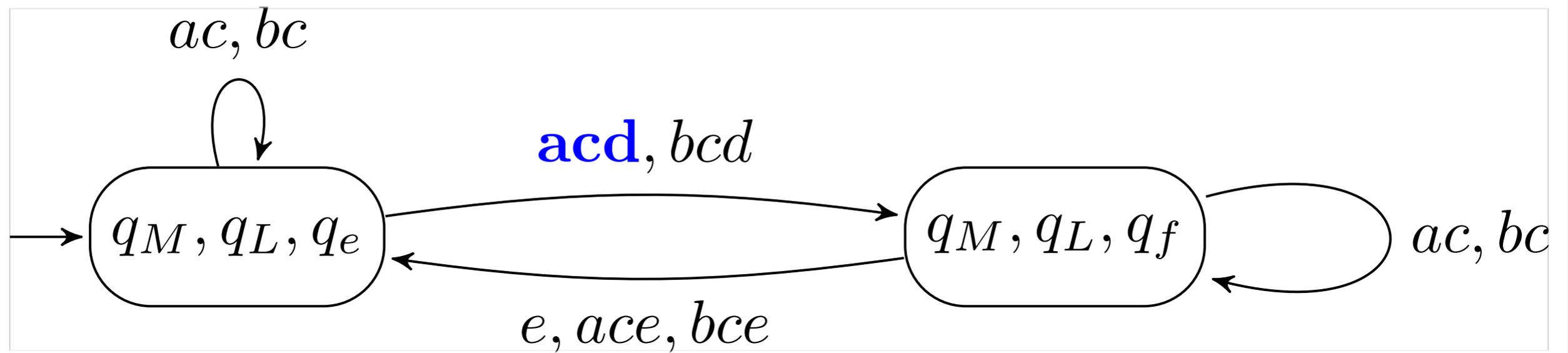
$$\{cl_1 \bowtie cl_2 \mid cl_1 \in CT_1, cl_2 \in CT_2, cl_1 \frown cl_2\}$$

$$cl_1 \frown cl_2 = \forall e \in \text{dom}(cl_1) \cap \text{dom}(cl_2) \cdot cl_1(e) = cl_2(e)$$

$$cl_1 \bowtie cl_2 = cl_1 \cup cl_2$$

Exercise: compose colouring tables





Port Automata

Connector behaviour (statefull)

- Dataflow behaviour is **discrete** in time: it can be observed and snapshots taken at a pace fast enough to obtain (at least) a snapshot as often as the configuration of the connector changes
- At each time unit the connector performs an **evaluation step**: it evaluates its configuration and according to its interaction constraints changes to another (possibly different) configuration
- A connector can **fire multiple ports in the same evaluation step**

Port Automata

$$A = (Q, \mathcal{N}, \rightarrow, Q_0)$$

Q

set of states

\mathcal{N}

a set of ports \mathcal{N}

$$\rightarrow \subseteq Q \times 2^{\mathcal{N}} \times Q$$

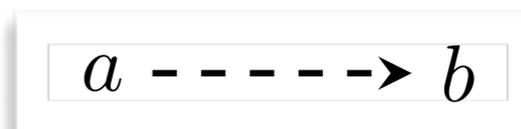
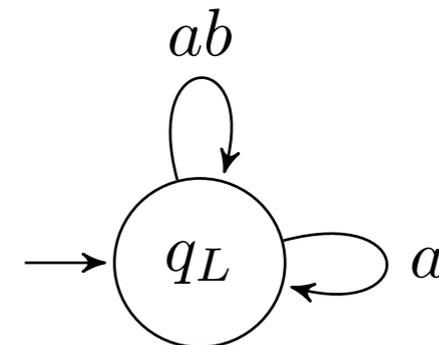
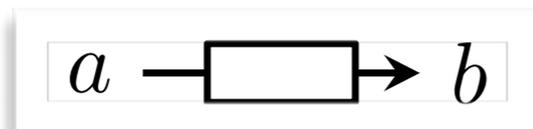
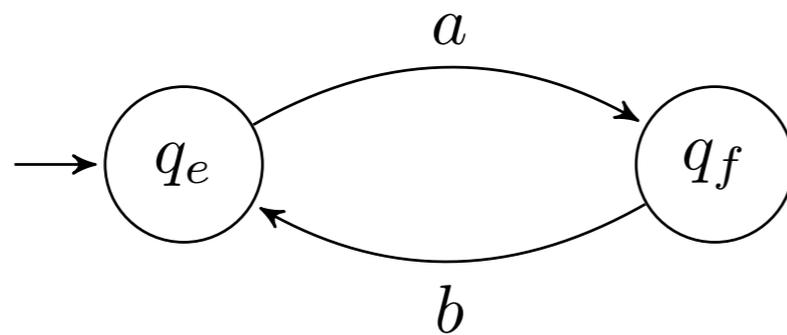
a transition relation

$$Q_0 \subseteq Q$$

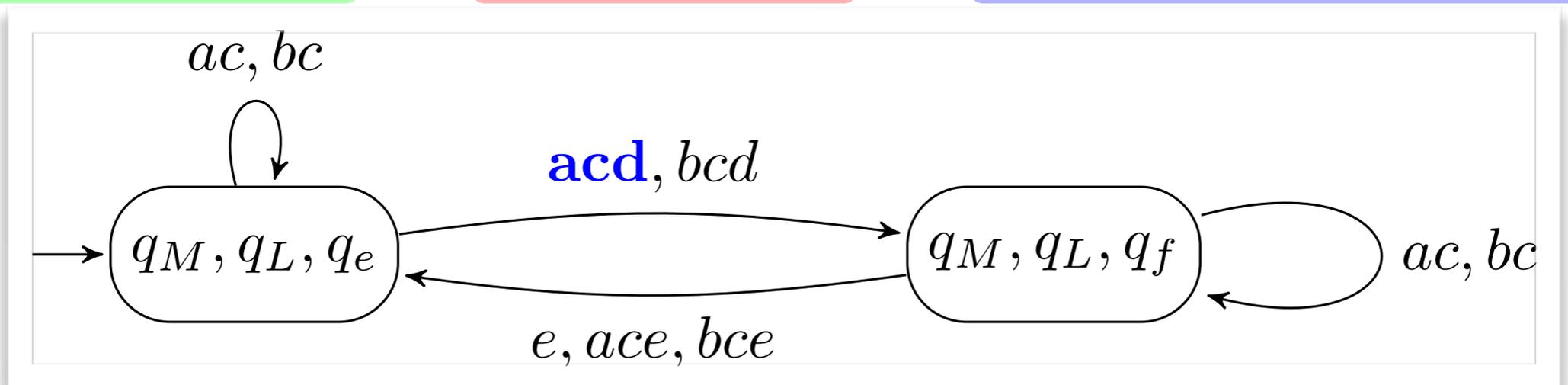
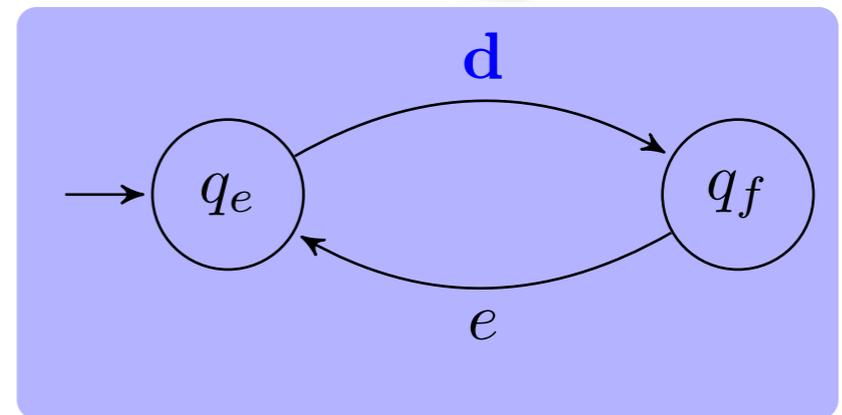
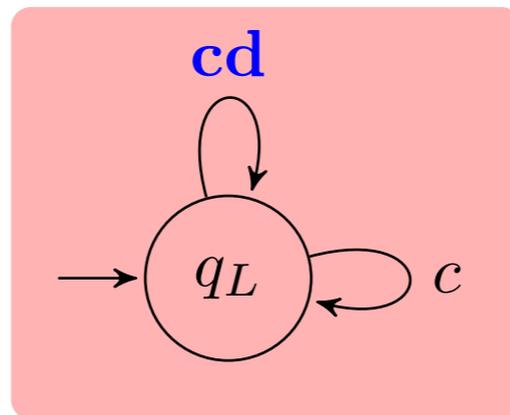
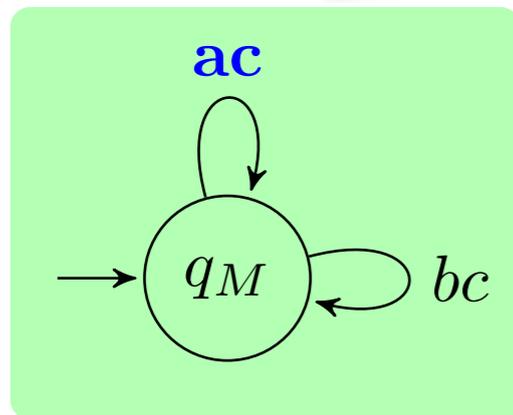
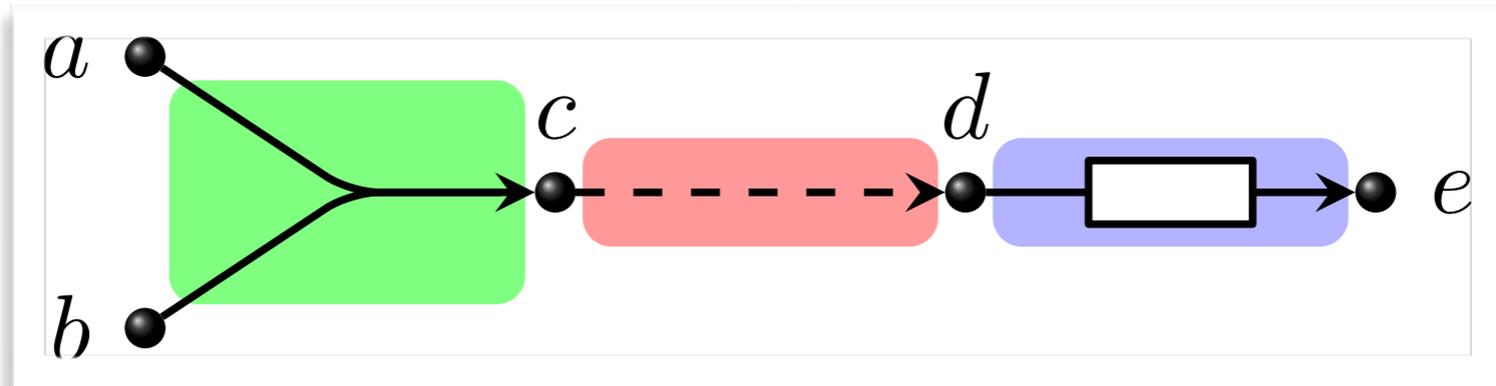
a set of initial states

transitions must have a non-empty set of ports!

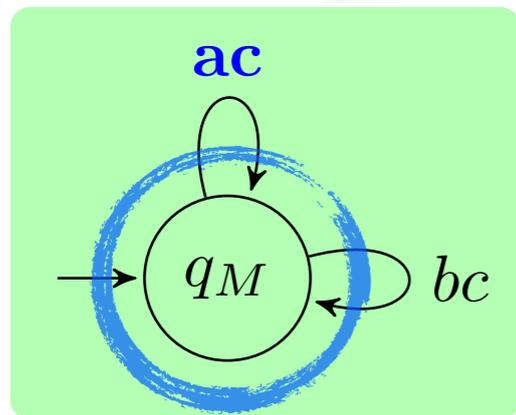
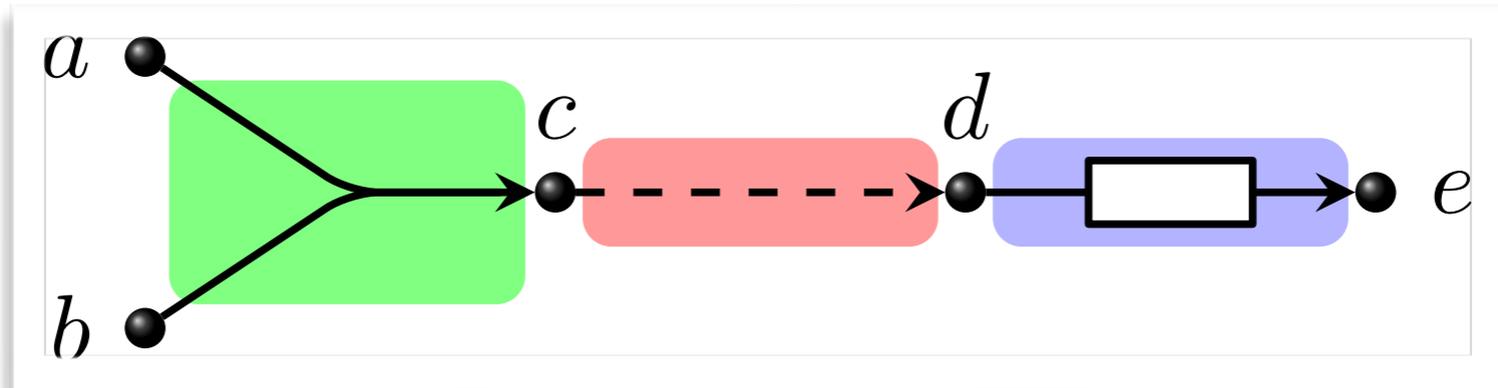
examples:



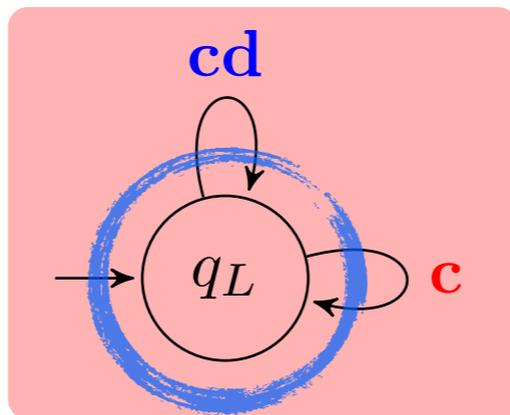
Composing steps



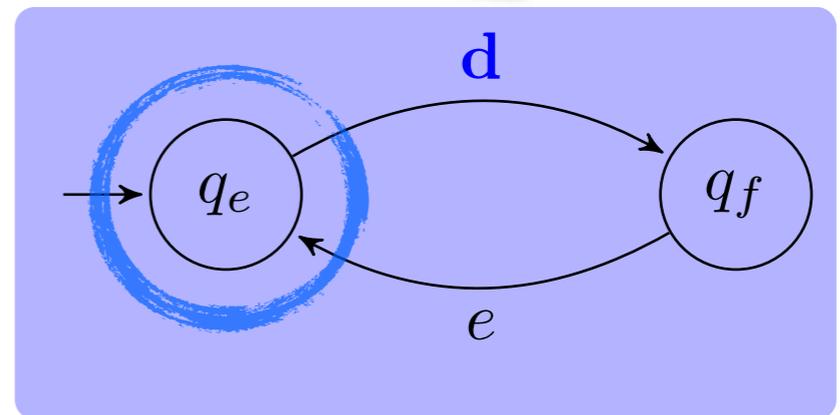
Composing steps



\bowtie



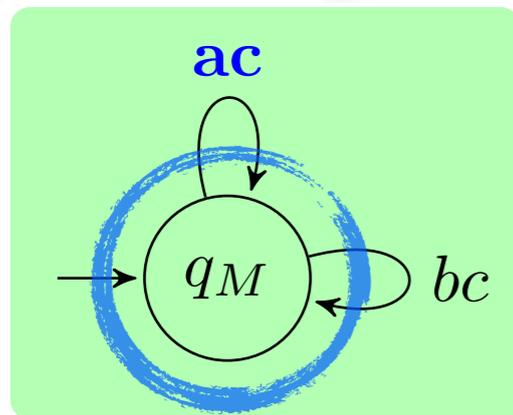
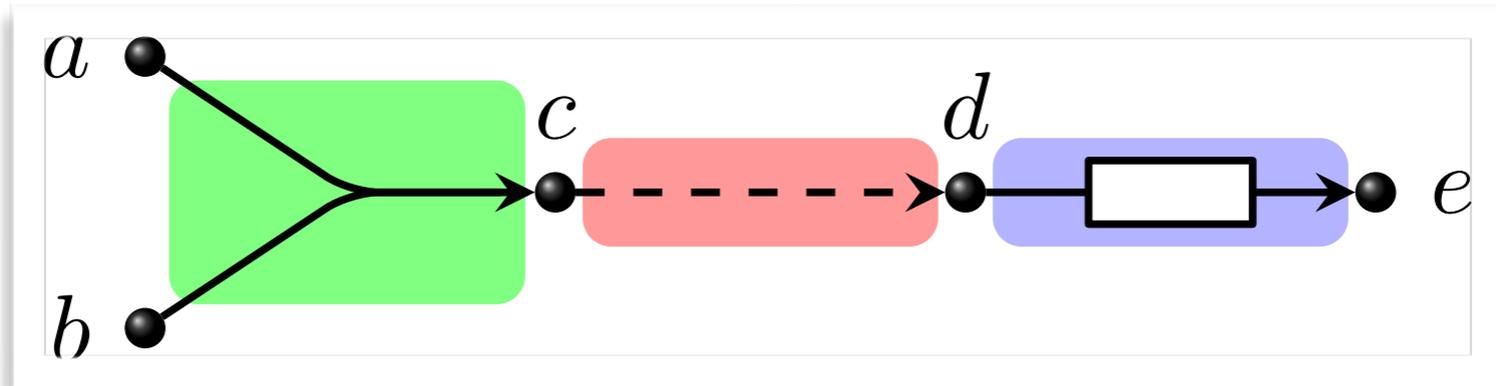
\bowtie



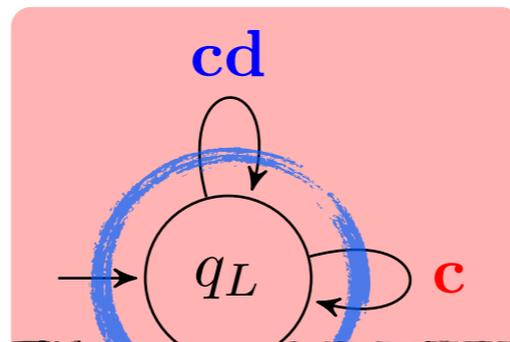
$$ac \bowtie cd \bowtie d = acd$$

$$ac \bowtie c \bowtie d = \perp$$

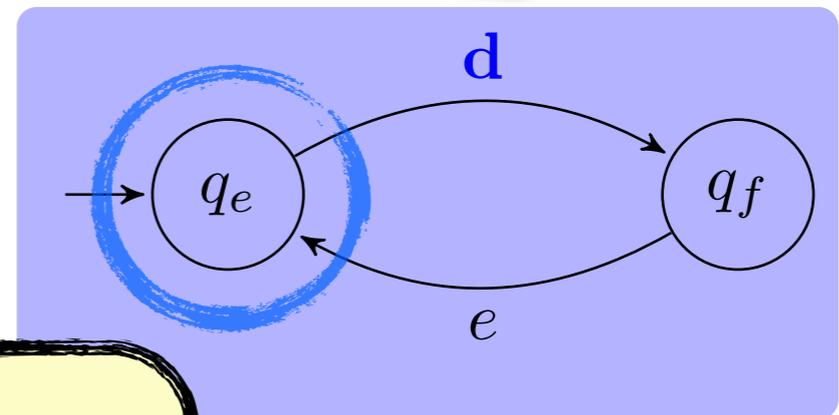
Composing steps



⊗



⊗



merger ; lossy ; fifo

JavaScript: <https://reolanguage.github.io/ReoLive/snapshot/>

Composition - formally

Definition 2. The product of two port automata $\mathcal{A}_1 = (\mathcal{Q}_1, \mathcal{N}_1, \rightarrow_1, \mathcal{Q}_{0,1})$ and $\mathcal{A}_2 = (\mathcal{Q}_2, \mathcal{N}_2, \rightarrow_2, \mathcal{Q}_{0,2})$ is defined by

$$\mathcal{A}_1 \bowtie \mathcal{A}_2 = (\mathcal{Q}_1 \times \mathcal{Q}_2, \mathcal{N}_1 \cup \mathcal{N}_2, \rightarrow, \mathcal{Q}_{0,1} \times \mathcal{Q}_{0,2})$$

where \rightarrow is defined by the rule

$$\frac{q_1 \xrightarrow{N_1}_1 p_1 \quad q_2 \xrightarrow{N_2}_1 p_2 \quad N_1 \cap \mathcal{N}_2 = N_2 \cap \mathcal{N}_1}{\langle q_1, q_2 \rangle \xrightarrow{N_1 \cup N_2} \langle p_1, p_2 \rangle}$$

and the following and its symmetric rule

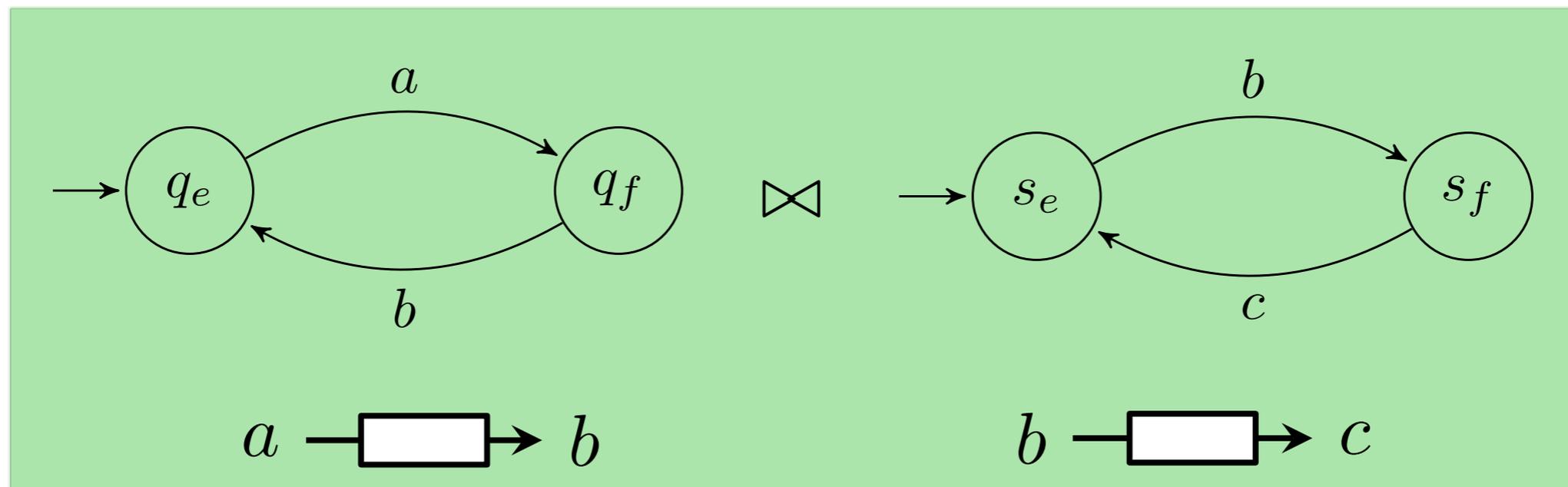
$$\frac{q_1 \xrightarrow{N_1}_1 p_1 \quad N_1 \cap \mathcal{N}_2 = \emptyset}{\langle q_1, q_2 \rangle \xrightarrow{N_1} \langle p_1, q_2 \rangle}$$

Formalize and compose

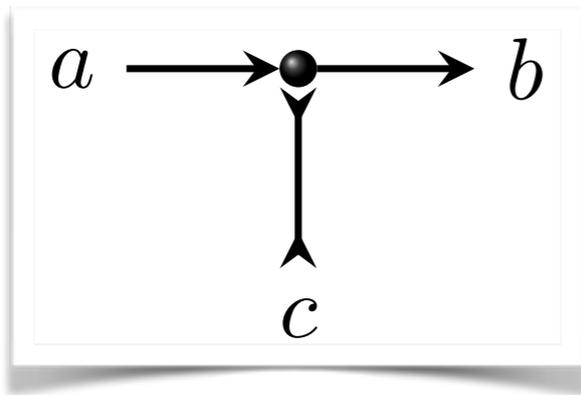
$$\frac{q_1 \xrightarrow{N_1}_1 p_1 \quad q_2 \xrightarrow{N_2}_1 p_2 \quad N_1 \cap \mathcal{N}_2 = N_2 \cap \mathcal{N}_1}{\langle q_1, q_2 \rangle \xrightarrow{N_1 \cup N_2} \langle p_1, p_2 \rangle}$$

$$\frac{q_1 \xrightarrow{N_1}_1 p_1 \quad N_1 \cap \mathcal{N}_2 = \emptyset}{\langle q_1, q_2 \rangle \xrightarrow{N_1} \langle p_1, q_2 \rangle}$$

$$\mathcal{A} = (\mathcal{Q}, \mathcal{N}, \rightarrow, \mathcal{Q}_0)$$

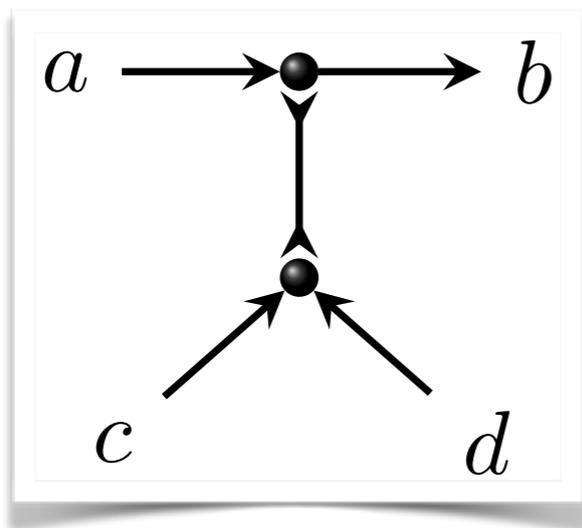


Examples I



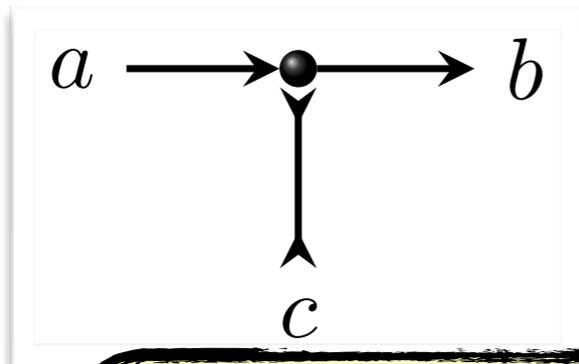
Flow regulator

"c" controls flow from "a" to "b"



data flows from "a" to "b" ONLY if either "c" or "d" have data

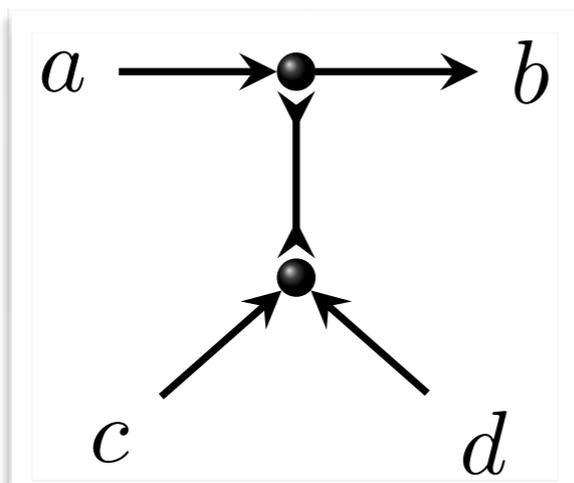
Examples I



Flow regulator

"b" controls flow from "a" to "c"

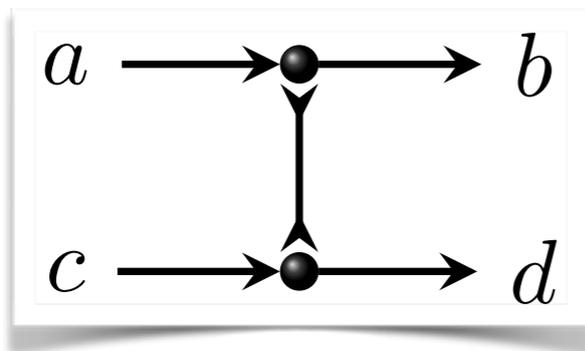
`dupl*id ; id*drain`



data flows from "a" to "b" ONLY if either "c" or "d" have data

`dupl*merger ; id*drain`

Examples II

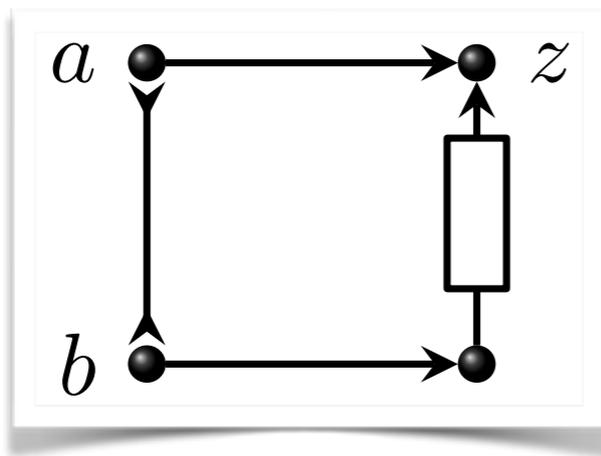


Synchronising barrier

data flows "a" \longrightarrow "b"

IFF

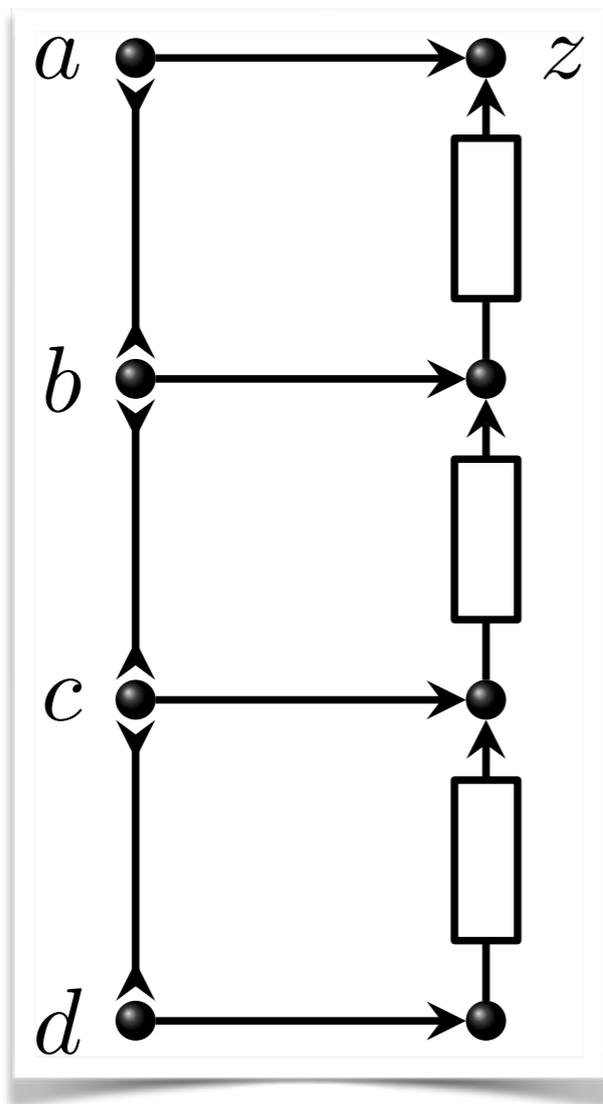
data flows "c" \longrightarrow "d"



Alternator

data flows from "a"
and from "b" to "z",
alternating (+ extra
synch constraints)

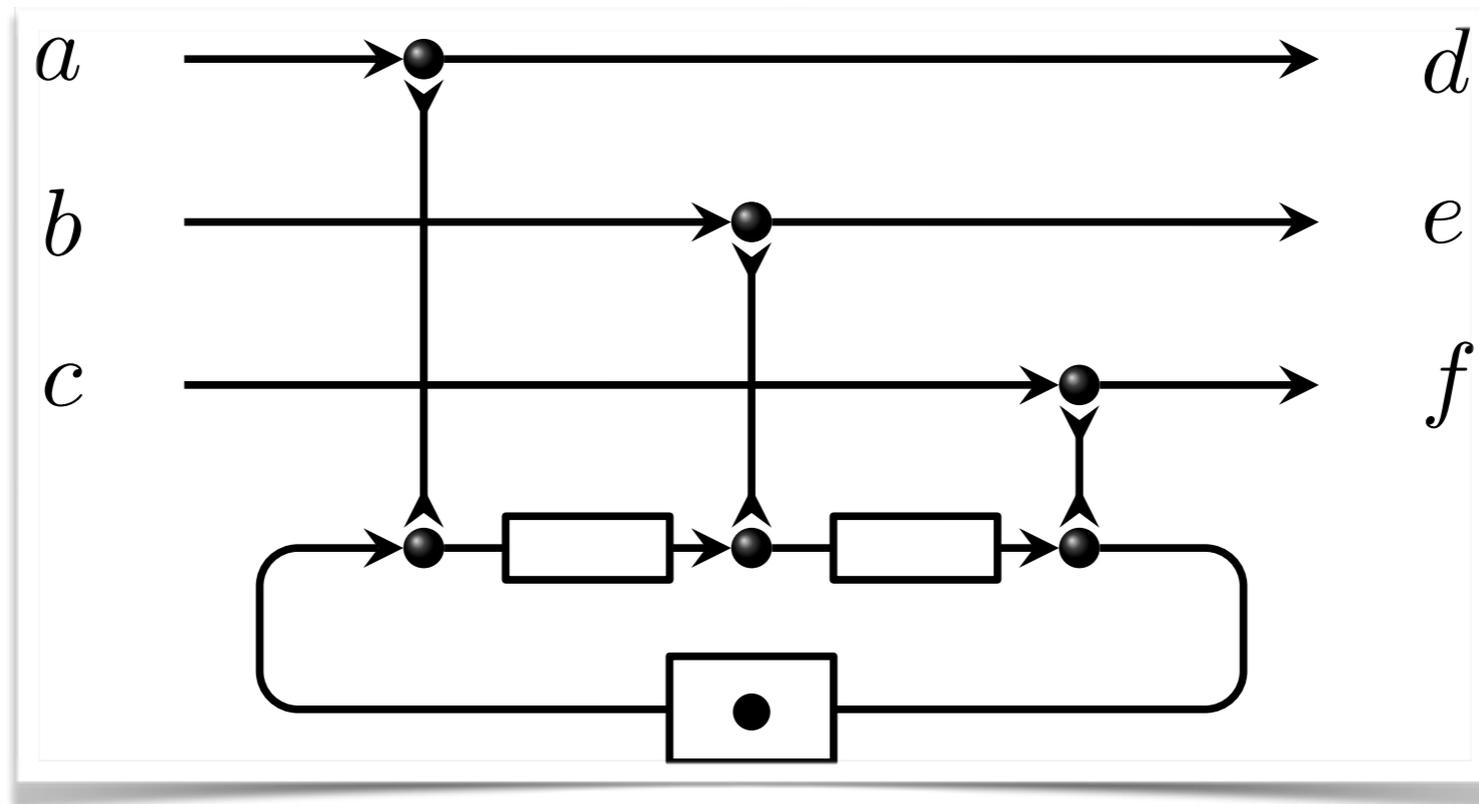
Examples III



N-Alternator

data flows from "a", "b", "c", and "d" to "z", alternating (+ extra synch constraints)

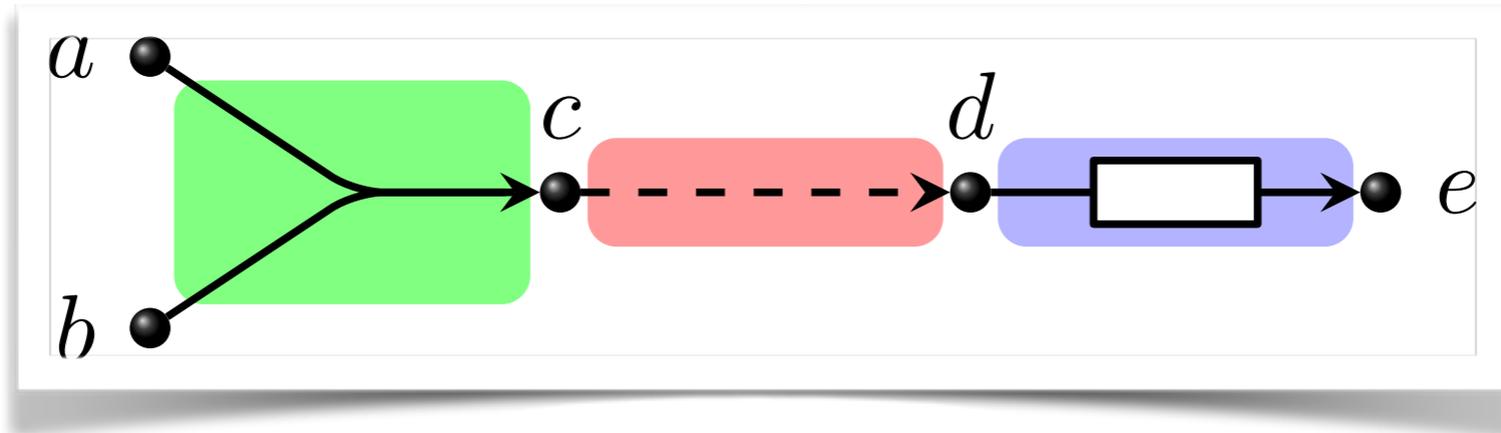
Examples IV



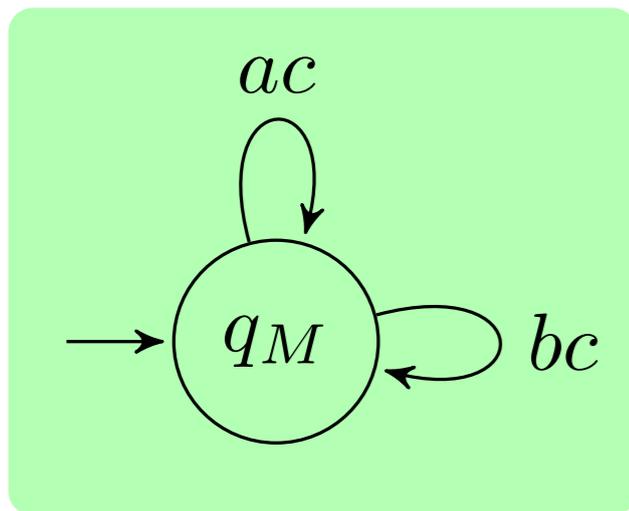
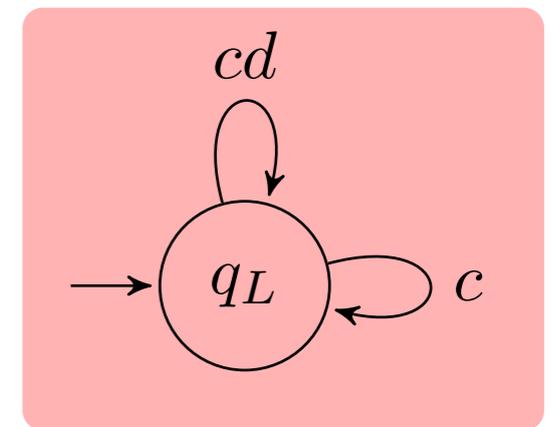
Sequencer

Data flows from "a" to "d", "b" to "e", and "c" to "f" alternating.

Reo in mCRL2

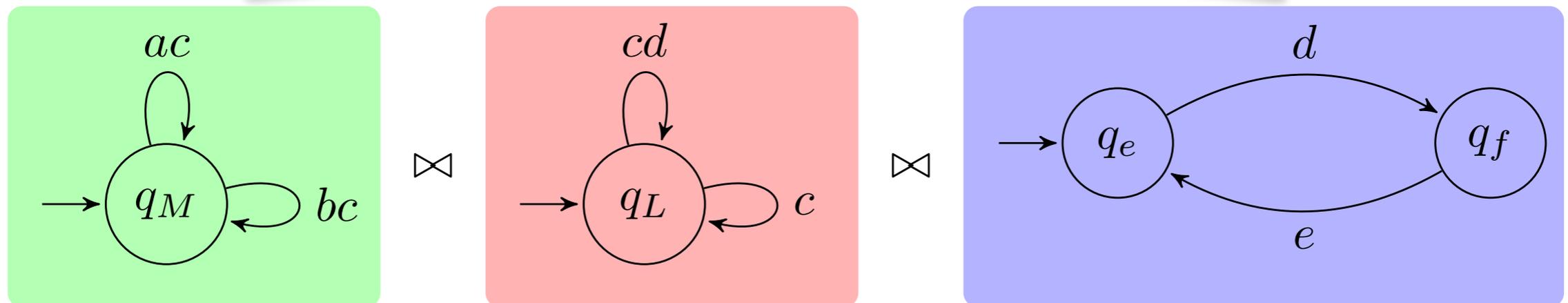
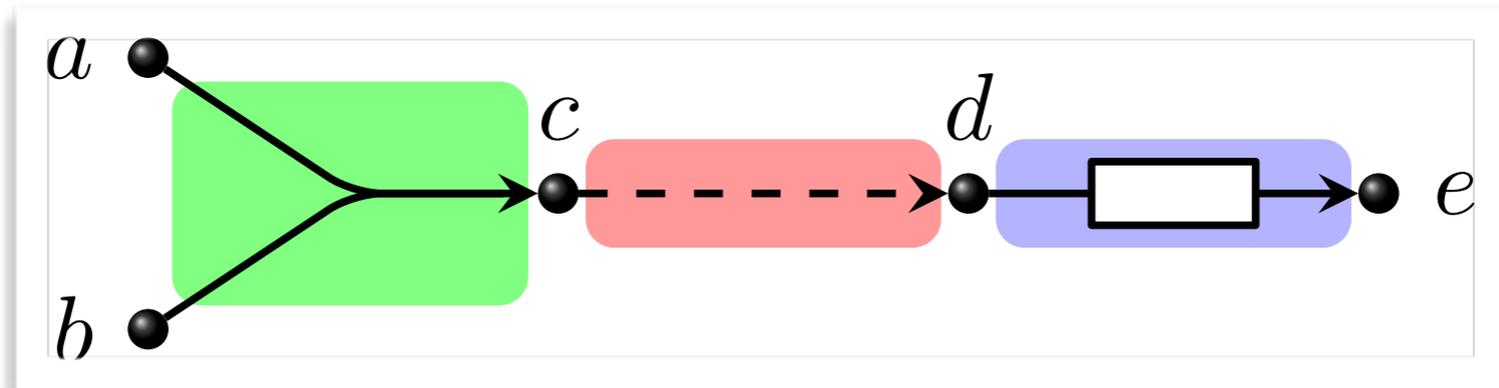


$$\text{Lossy} = (c|d + c).\text{Lossy}$$



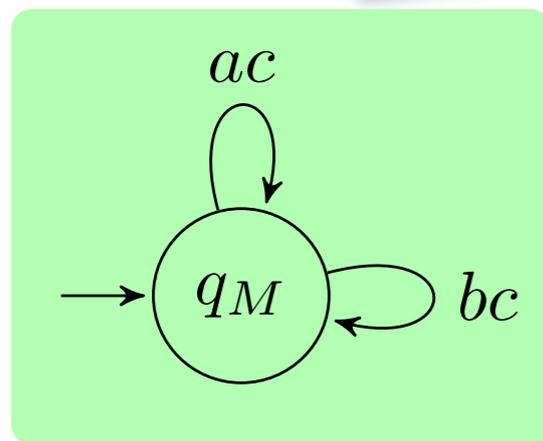
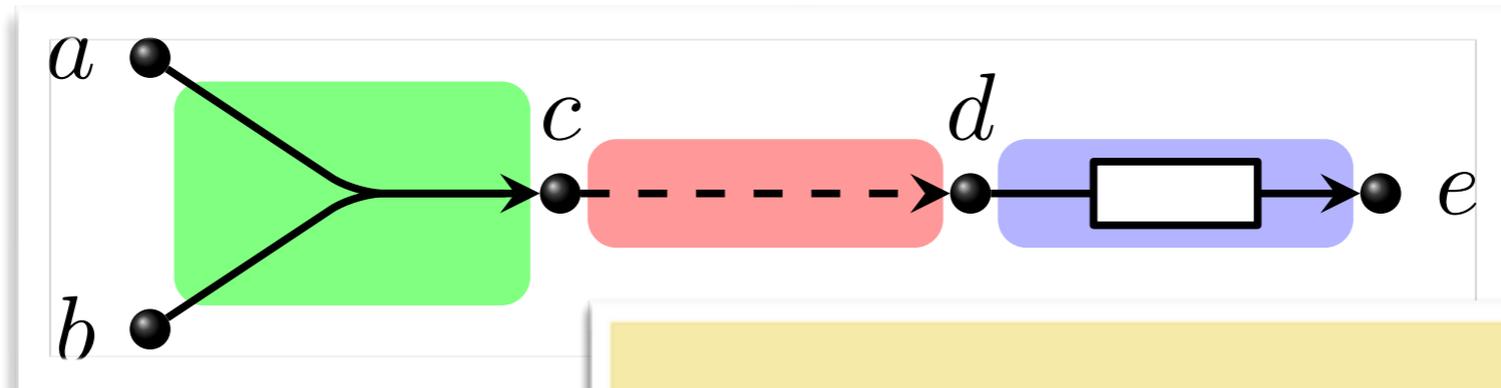
$$\text{Merger} = (a|c + b|c).\text{Merger}$$

Reo in mCRL2

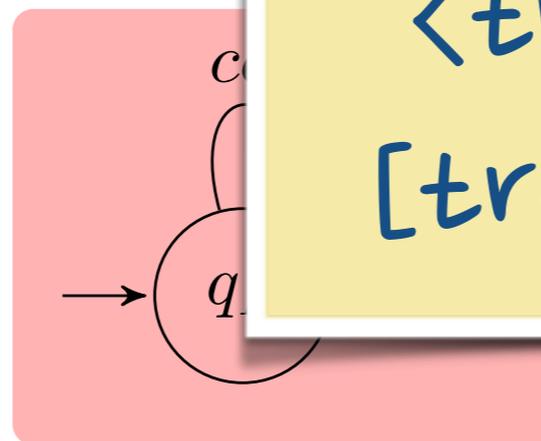


Conn = hide($\{c, d\}$,
 block($\{c_1, c_2, d_1, d_2\}$,
 comm($\{c_1|c_2 \rightarrow c, d_1|d_2 \rightarrow d\}$,
 Merger || Lossy || FIFO1)))

Reo in mCRL2



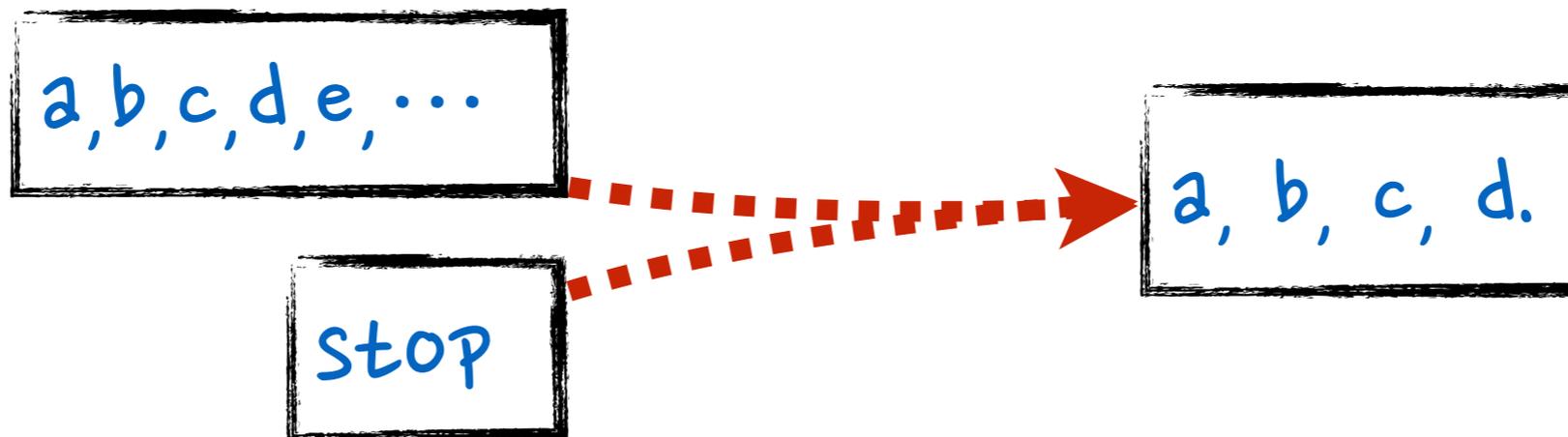
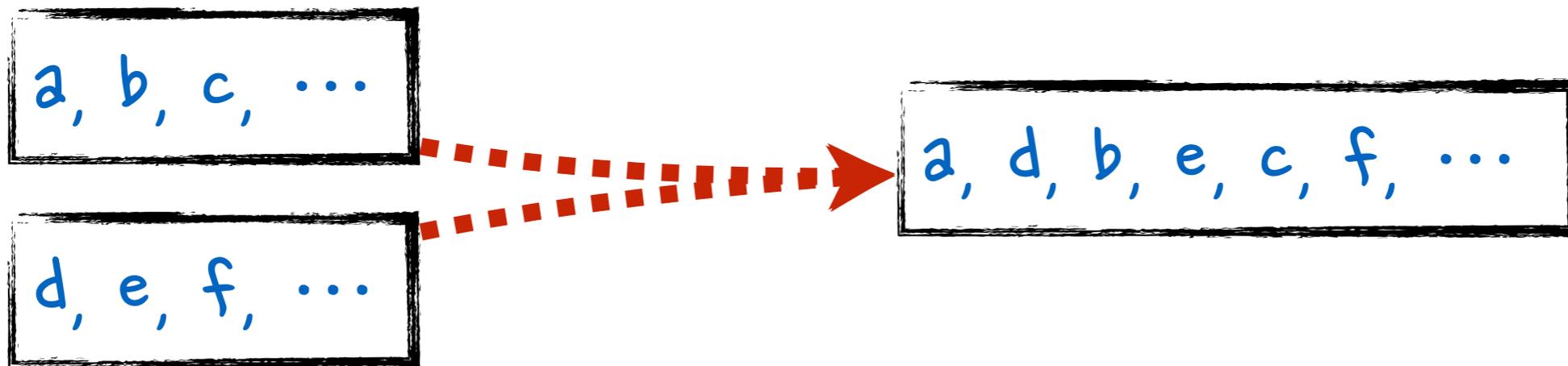
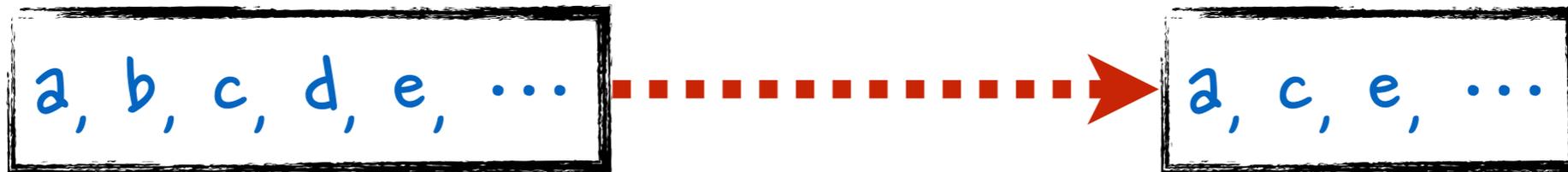
\boxtimes



$\langle \text{true}^*.a|c|d|e \rangle \text{true}$
 $[\text{true}^*.a|c|d|e.e] \text{false}$

Conn = hide($\{c,d\}$,
 block($\{c_1,c_2,d_1,d_2\}$,
 comm($\{c_1|c_2 \rightarrow c, d_1|d_2 \rightarrow d\}$,
 Merger || Lossy || FIFO1)))

Build connectors



Can you prove?

colourings and port automata provide equivalent semantics

$$\mathcal{A}(C_1) = (Q_1, \mathcal{N}_1, \rightarrow_1, q_{0,1})$$

$$\mathcal{A}(C_2) = (Q_2, \mathcal{N}_2, \rightarrow_2, q_{0,2})$$

$\mathcal{CT}(C)$ – colouring table of C

$col(q \xrightarrow{P} q')$ – colouring associated to a transition

$$(\langle q_{0,1}, q_{0,2} \rangle \xrightarrow{P} \langle q_1, q_2 \rangle) \in \mathcal{A}(C_1) \bowtie \mathcal{A}(C_2)$$

\Rightarrow

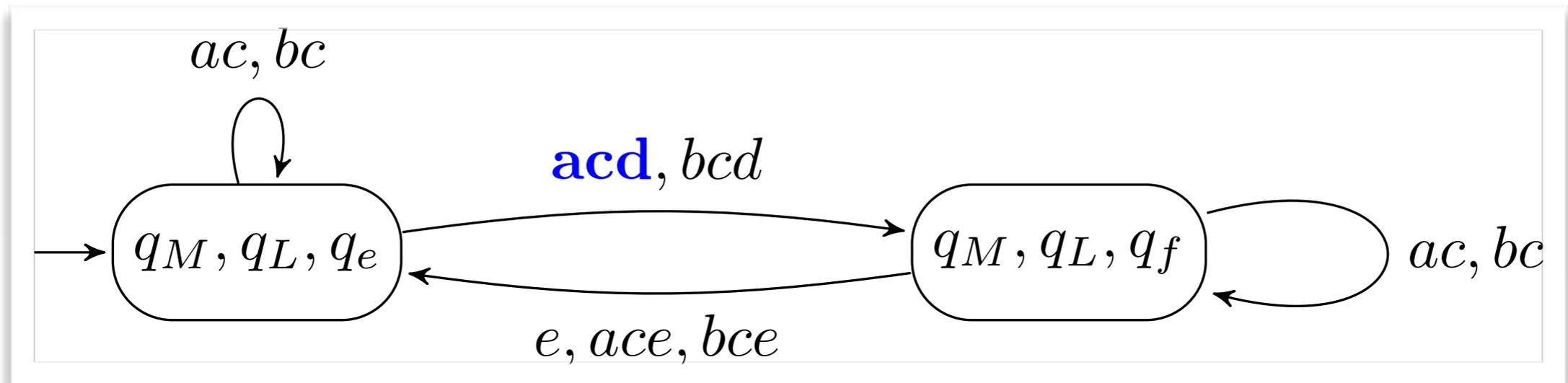
$$col(\langle q_{0,1}, q_{0,2} \rangle \xrightarrow{P} \langle q_1, q_2 \rangle) \in \mathcal{CT}(C_1) \bowtie \mathcal{CT}(C_2)$$

Can you prove? (more generically)

colourings and port automata provide equivalent semantics

$$A = (\mathcal{Q}, \mathcal{N}, \rightarrow, \{q_0\})$$

$$\begin{aligned} (q_0 \xrightarrow{P} q) \in \mathcal{A}(C) \\ \Rightarrow \\ \text{col}(P, \mathcal{N}) \in \mathcal{CT}(C) \end{aligned}$$



Constraint Automata

Constraint Automata

Automata labelled by

- a **data constraint** which represents a set of data assignments to port names

$$g ::= \text{true} \mid d_A = v \mid g_1 \vee g_2 \mid \neg g$$

Over Data and Ports

Note: other constraints, such as

$$d_A = d_B \stackrel{\text{abv}}{=} \bigvee_{d \in \text{Data}} (d_A = d \wedge d_B = d)$$

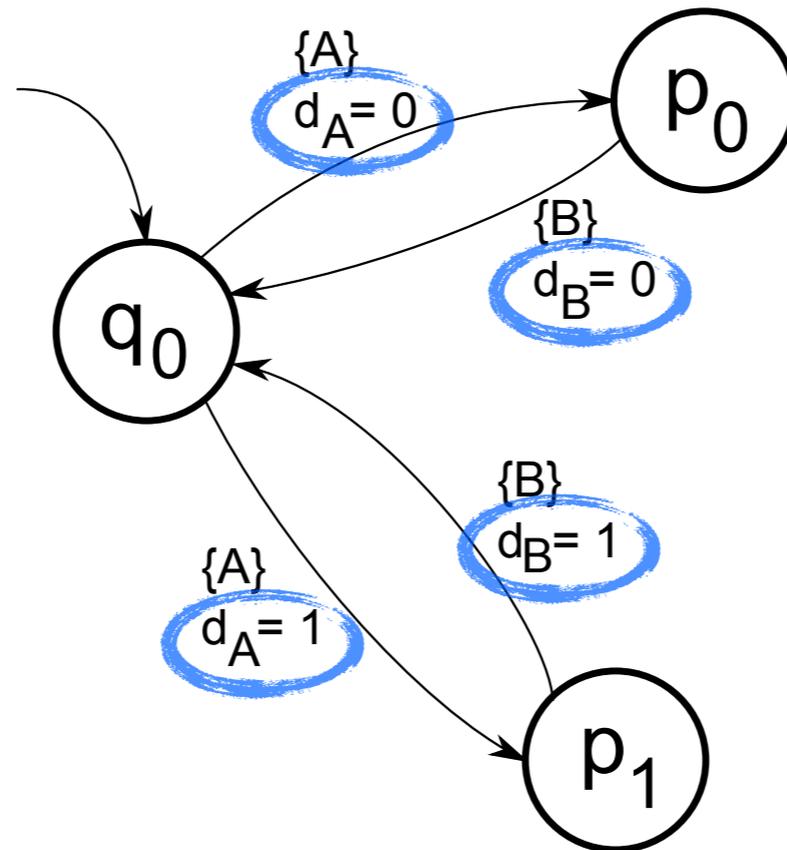
are derived.

- a **name set** which represents the set of port names at which IO can occur

States represent the configurations of the corresponding connector, while transitions encode its maximally-parallel stepwise behaviour.

Constraint Automata

Example: FIFO1



Constraint Automata - Definition

$$A = (Q, \mathcal{N}, \rightarrow, Q_0)$$

Q

set of states

\mathcal{N}

a set of ports \mathcal{N}

$Q_0 \subseteq Q$

a set of initial states

$\rightarrow \subseteq Q \times 2^{\mathcal{N}} \times DC \times Q$

a transition relation such that $\xrightarrow{P, g}$ iff

1. $P \neq \emptyset$

2. $g \in DC(P, Data)$

$(DC(P, Data))$ is the set of data constraints over Data and P)

Constraint Automata - Definition

$s \xrightarrow{P,g} s'$ iff

1. $P \neq \emptyset$
2. $g \in DC(P, Data)$

in configuration s , ports in P can perform IO operations which meet guard g and lead to s'

transitions fire only if data occurs at a (set of) ports P

behaviour depends only on observed data
(not on future evolution)

Constraint Automata as a semantics for Reo

- cannot capture **context-awareness** [Baier, Sirjani, Arbab, Rutten 2006], but forms the basis for more elaborated models (eg, **Reo automata**)
- captures all behaviour alternatives of a connector; useful to generate a state-machine implementing the connector's behaviour
- basis for several tools, including the model checker **Vereofy** [Kluppelholz, Baier 2007]

Constraint Automata - Reo connectors

$$\circ \rightleftarrows \{A, B\} \ d_A = d_B$$

$$A \longrightarrow B$$

Sync

$$\circ \rightleftarrows \{A, B\}$$

$$A \rightleftarrows B$$

SyncDrain

$$\{A\} \rightleftarrows \circ \rightleftarrows \{A, B\} \ d_A = d_B$$

$$A \dashrightarrow B$$

LossySync

$$\{A\} \neg \text{expr}(d_A) \rightleftarrows \circ \rightleftarrows \{A, B\} \ \text{expr}(d_A) \wedge d_A = d_B$$

$$A \rightsquigarrow B$$

Filter

$$\{A, C\} \ d_A = d_C \rightleftarrows \circ \rightleftarrows \{B, C\} \ d_B = d_C$$

$$\begin{array}{c} A \\ B \end{array} \rightarrow C$$

Merger

$$\circ \rightleftarrows \{A, B, C\} \ d_A = d_B = d_C$$

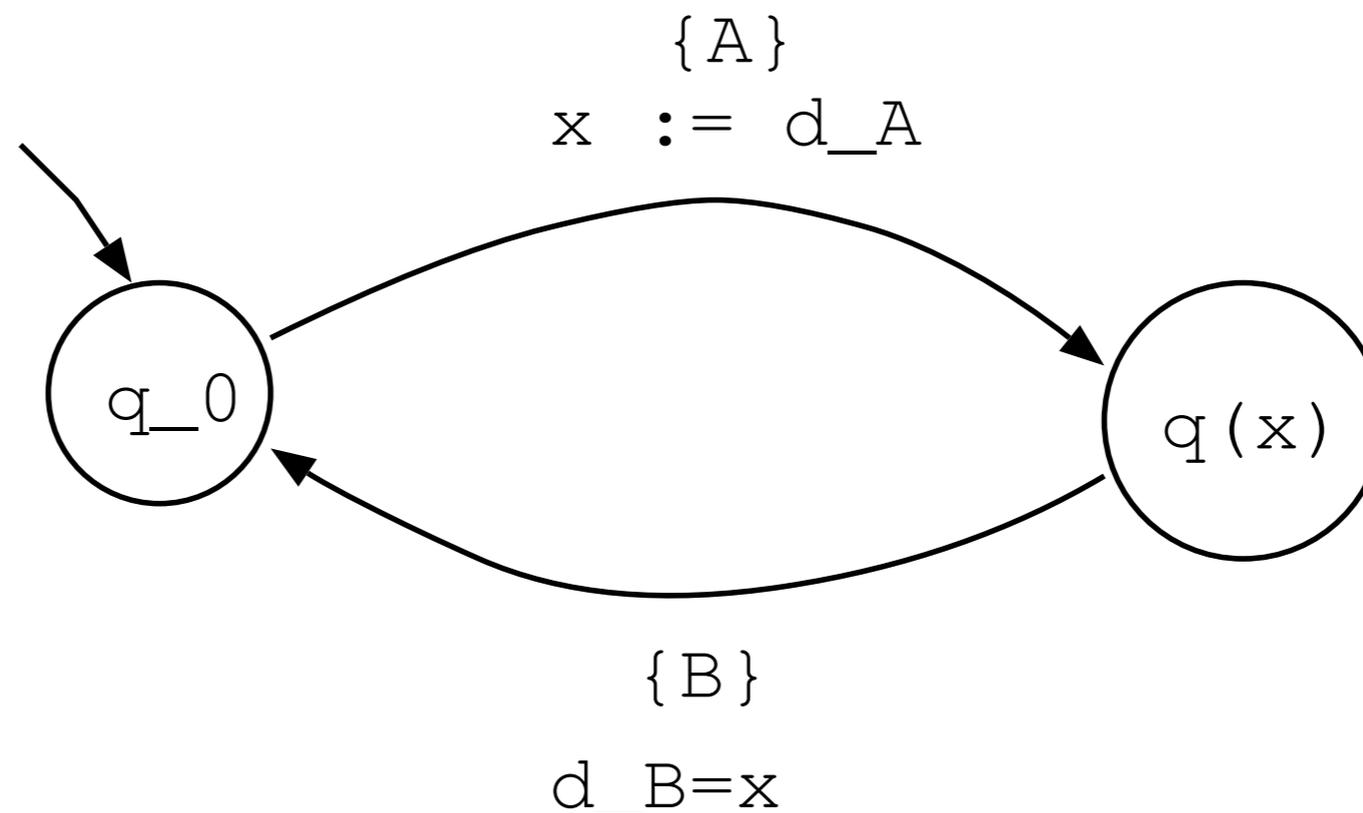
$$A \rightarrow \begin{array}{c} B \\ C \end{array}$$

Replicator

[Parameterised constraint automata]

States are parametric on data values ... therefore capturing complex constraint automata emerging from data-dependencies

Example: 1 bounded FIFO



[Parameterised constraint automata]

$$\mathcal{L} = (\mathcal{L}, \mathcal{N}, \mathcal{V}, \rightarrow, \mathcal{L}_0, \text{init})$$

\mathcal{L}

set of locations

\mathcal{N}

a set of ports

\mathcal{V}

a set of variables

$\mathcal{L}_0 \subseteq \mathcal{L}$

a set of initial states

init

an initialisation of variables

$$\rightarrow \subseteq \mathcal{L} \times 2^{\mathcal{N}} \times DC \times \text{Assgn} \times \mathcal{L}$$

a transition relation such that $\xrightarrow{P,g,h}$ iff

1. $P \neq \emptyset$

2. $g \in DC(P, \text{Data}, \mathcal{V})$

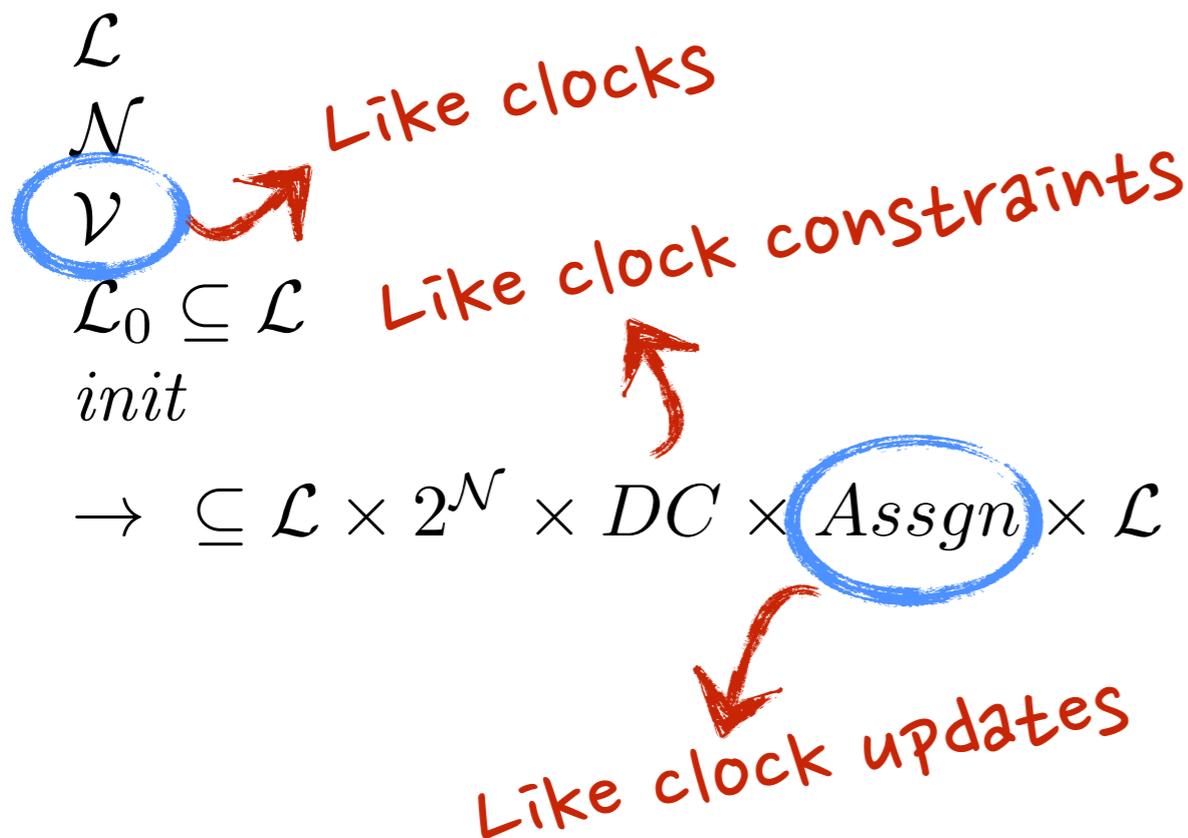
3. $h \in \mathcal{V} \rightarrow \text{Expr}(P, \text{Data}, \mathcal{V})$

($DC(P, \text{Data}, \mathcal{V})$ is the set of data constraints over Data, P, and \mathcal{V})

($\text{Expr}(P, \text{Data}, \mathcal{V})$ is an expression over Data, P, and \mathcal{V})

[Parameterised constraint automata]

$$\mathcal{L} = (\mathcal{L}, \mathcal{N}, \mathcal{V}, \rightarrow, \mathcal{L}_0, \text{init})$$



set of locations

a set of ports

a set of variables

a set of initial states

an initialisation of variables

a transition relation such that $\xrightarrow{P,g,h}$ iff

1. $P \neq \emptyset$

2. $g \in DC(P, \text{Data}, \mathcal{V})$

3. $h \in \mathcal{V} \rightarrow \text{Expr}(P, \text{Data}, \mathcal{V})$

($DC(P, \text{Data}, \mathcal{V})$ is the set of data constraints over Data, P, and \mathcal{V})

($\text{Expr}(P, \text{Data}, \mathcal{V})$ is an expression over Data, P, and \mathcal{V})

Composing constraint automata

Definition 4.1 [*Product-automaton*] The product-automaton of the two constraint automata $\mathcal{A}_1 = (Q_1, \mathcal{N}ames_1, \longrightarrow_1, Q_{0,1})$ and $\mathcal{A}_2 = (Q_2, \mathcal{N}ames_2, \longrightarrow_2, Q_{0,2})$, is:

$$\mathcal{A}_1 \bowtie \mathcal{A}_2 = (Q_1 \times Q_2, \mathcal{N}ames_1 \cup \mathcal{N}ames_2, \longrightarrow, Q_{0,1} \times Q_{0,2})$$

where \longrightarrow is defined by the following rules:

$$\frac{q_1 \xrightarrow{N_1, g_1} p_1, \quad q_2 \xrightarrow{N_2, g_2} p_2, \quad N_1 \cap \mathcal{N}ames_2 = N_2 \cap \mathcal{N}ames_1}{\langle q_1, q_2 \rangle \xrightarrow{N_1 \cup N_2, g_1 \wedge g_2} \langle p_1, p_2 \rangle}$$

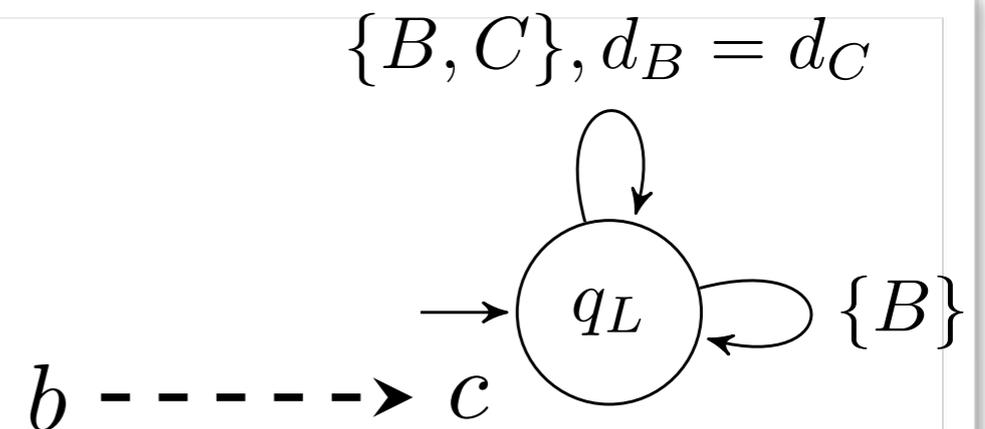
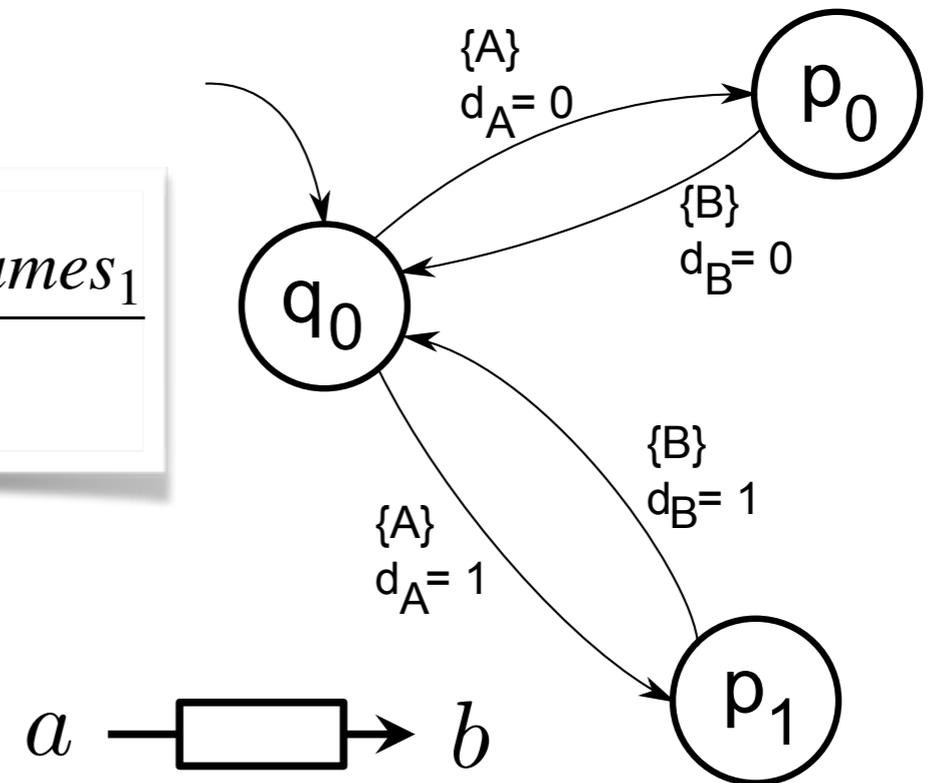
and

$$\frac{q_1 \xrightarrow{N, g} p_1, \quad N \cap \mathcal{N}ames_2 = \emptyset}{\langle q_1, q_2 \rangle \xrightarrow{N, g} \langle p_1, q_2 \rangle}$$

Formalize and compose

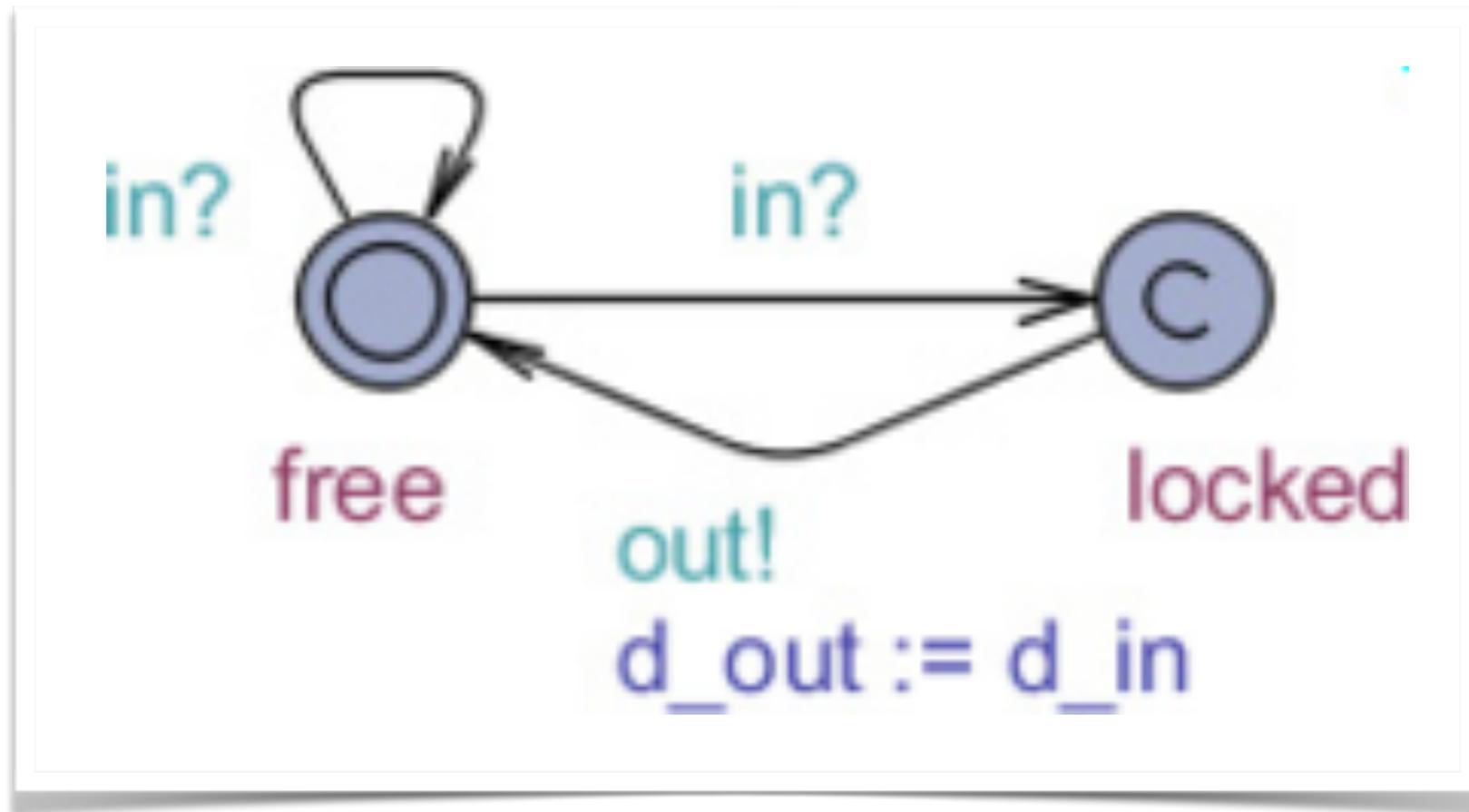
$$\frac{q_1 \xrightarrow{N_1, g_1} p_1, \quad q_2 \xrightarrow{N_2, g_2} p_2, \quad N_1 \cap \mathcal{N}ames_2 = N_2 \cap \mathcal{N}ames_1}{\langle q_1, q_2 \rangle \xrightarrow{N_1 \cup N_2, g_1 \wedge g_2} \langle p_1, p_2 \rangle}$$

$$\frac{q_1 \xrightarrow{N, g} p_1, \quad N \cap \mathcal{N}ames_2 = \emptyset}{\langle q_1, q_2 \rangle \xrightarrow{N, g} \langle p_1, q_2 \rangle}$$



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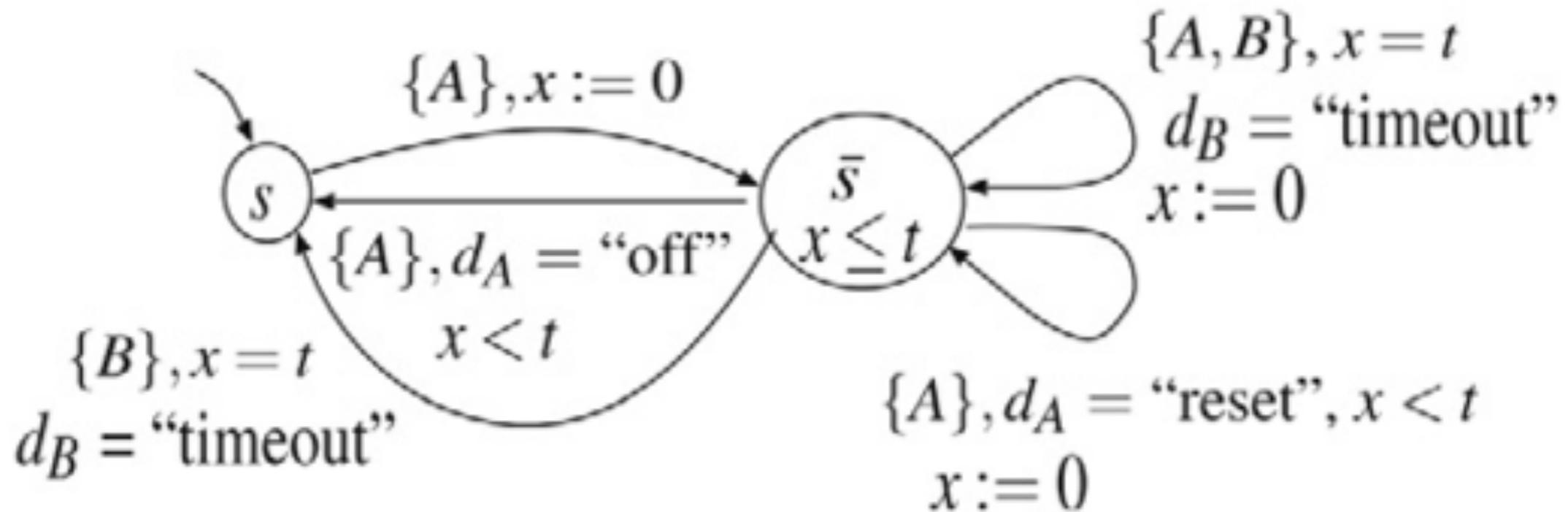
Formalism	Synchr.	Data	Time	Context	Partial
Connector Colouring	CC2	-		CC3	-
Automata	Port Automata	Constraint Automata	Time CA	-	-
Constraint s	✓	✓	x	✓	✓



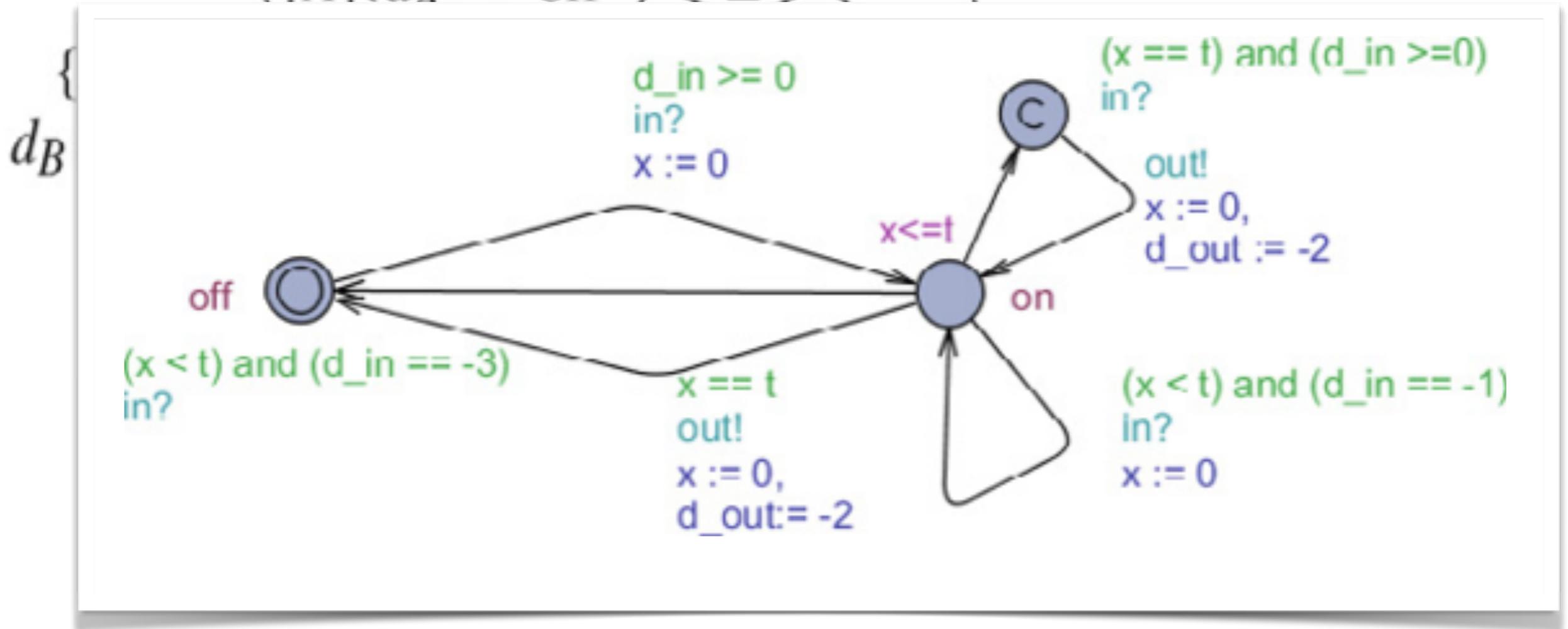
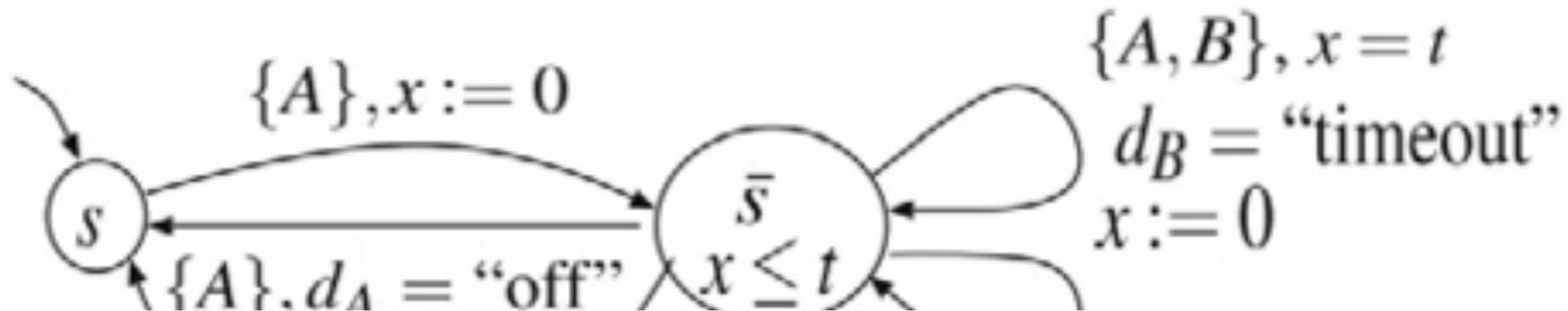
Timed Port/Const. Automata

Natallia Kokash, Mohammad Mahdi Jaghoori, Farhad Arbab.
From Timed Reo Networks to Networks of Timed Automata. 2013

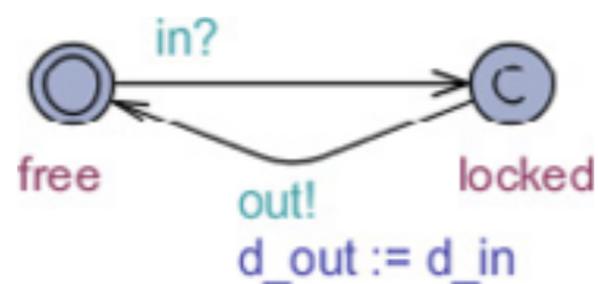
Timer (Data) Channel



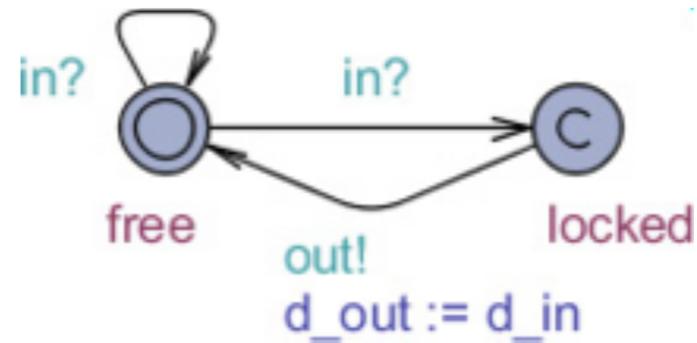
Timer (Data) Channel



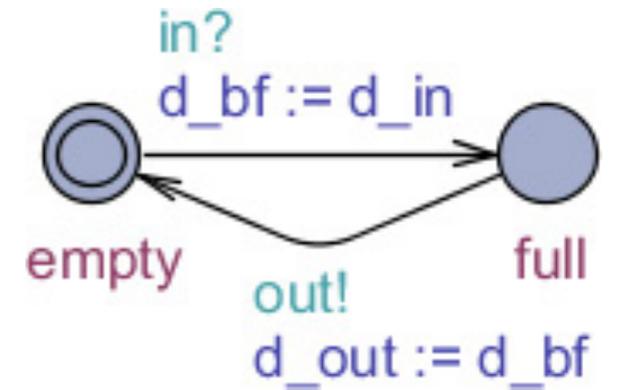
Time extension



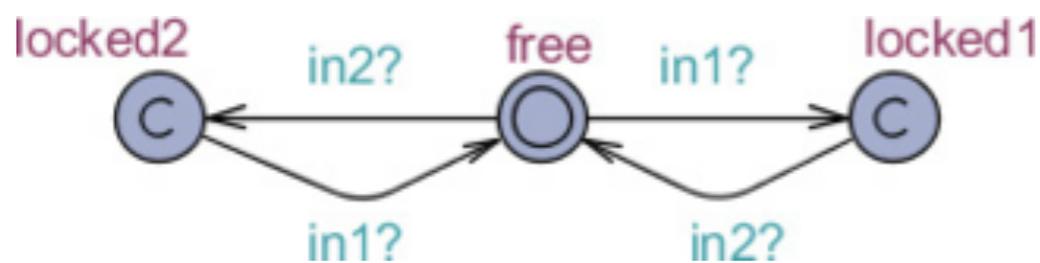
Sync



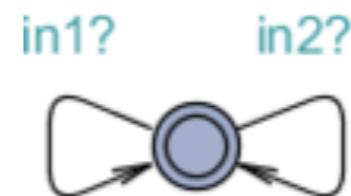
LossySync



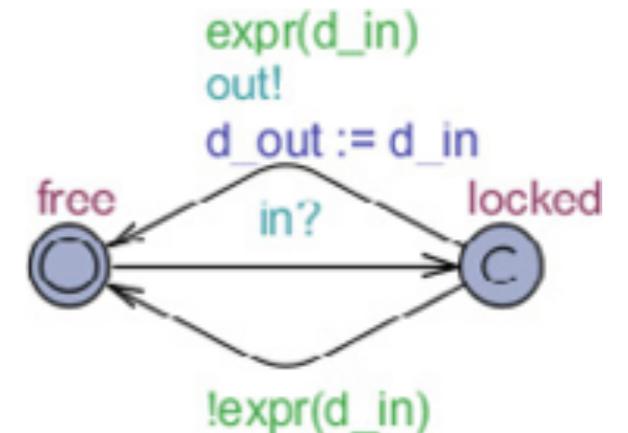
FIFO



SyncDrain



AsyncDrain



Filter

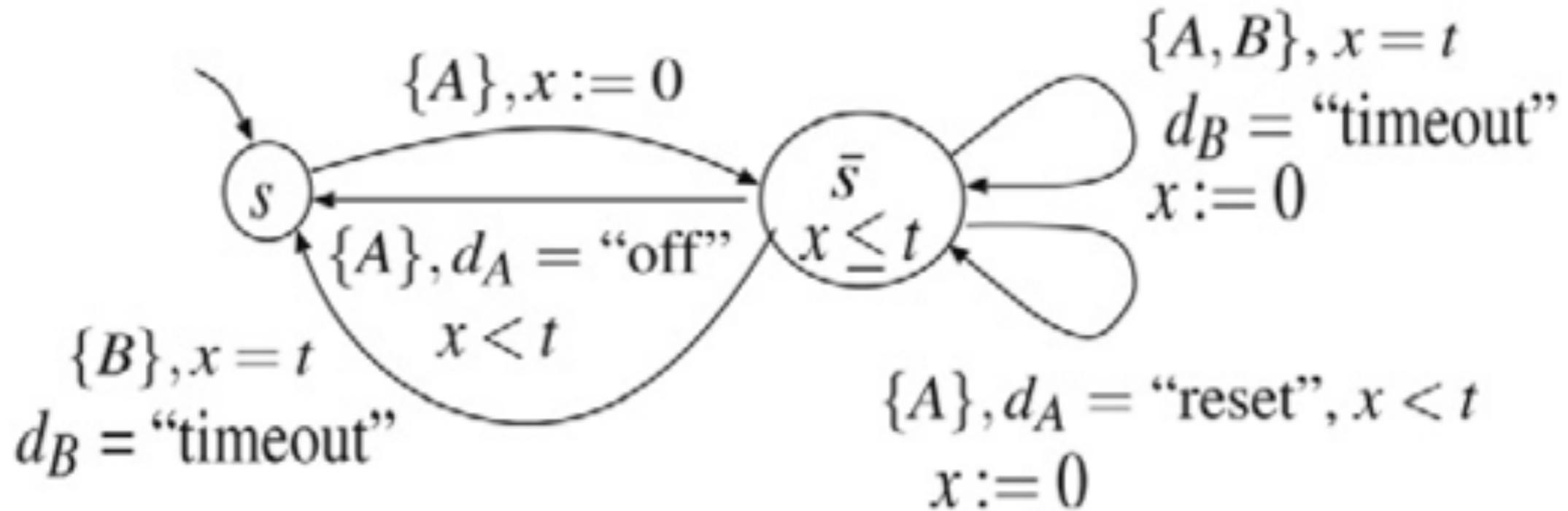
Formally

Definition 2.1 [Constraint automaton (CA)] A constraint automaton $\mathcal{A} = (S, \mathcal{N}, \rightarrow, s_0)$ consists of a set of states (also called locations) S , a set of port names \mathcal{N} , a transition relation $\rightarrow \subseteq S \times 2^{\mathcal{N}} \times DC \times S$, where DC is the set of data constraints over a finite data domain $Data$, and an initial state $s_0 \in S$.

Definition 2.2 [Timed constraint automaton (TCA) [3]] A TCA is an extended constraint automaton $\mathcal{A} = (S, \mathcal{N}, \rightarrow, s_0, \mathcal{C}, ic)$ with transition relation $\rightarrow \subseteq S \times 2^{\mathcal{N}} \times DC \times CC \times 2^{\mathcal{C}} \times S$ such that \mathcal{C} is a finite set of clocks and $ic : S \rightarrow CC$ is a function that assigns a clock constraint, called an invariance condition $ic(s)$ to each location s of \mathcal{A} .

without data!

Build channels (TCA)



$\text{delay}(t)$ - wait more than " t "
time (exclusive).

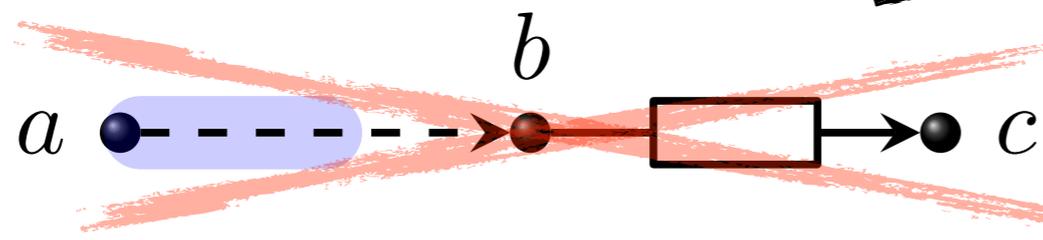
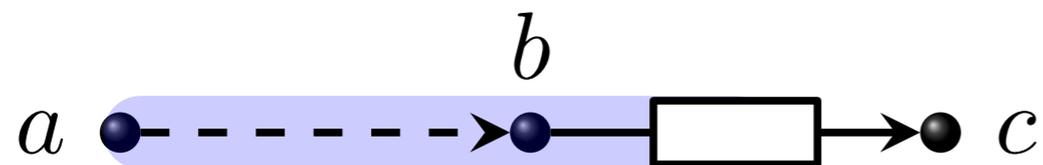
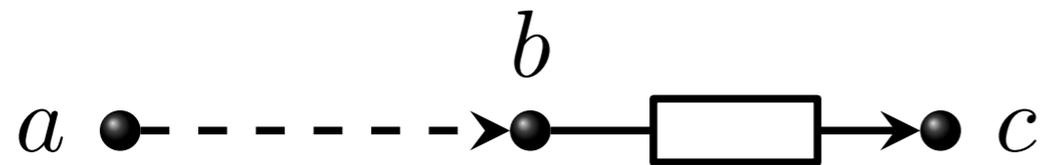
$\text{delayedTimer}(t)$ - wait between
" t_{\min} " and " t_{\max} ", inclusive.

$\text{timer}(t)$ - with "off" and
"reset" ports.

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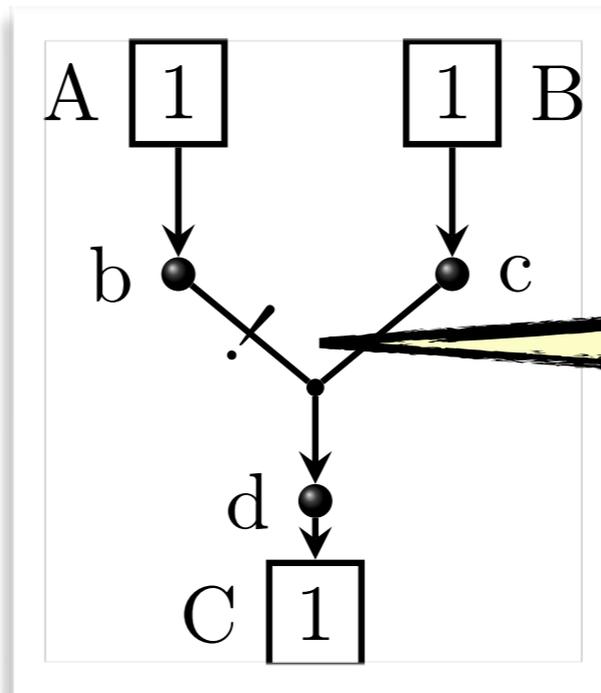
Formalism	Synchr.	Data	Time	Context	Partial
Connector Colouring	CC2	-		CC3	-
Automata	Port Automata	Constraint Automata	Time CA	-	-
Constraint s	✓	✓	x	✓	✓

2 reasons for context

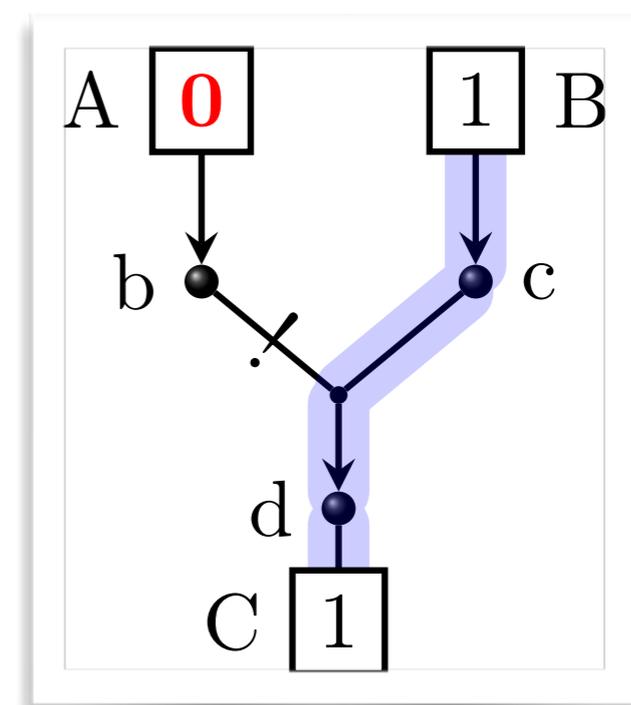
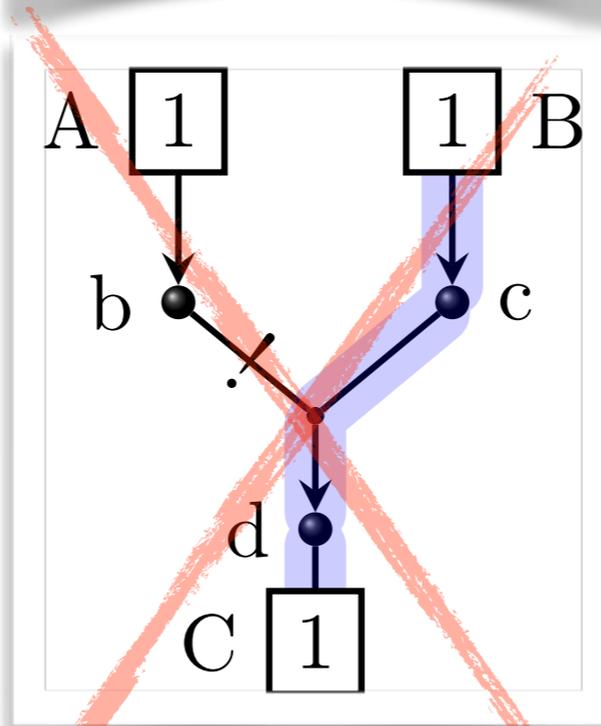
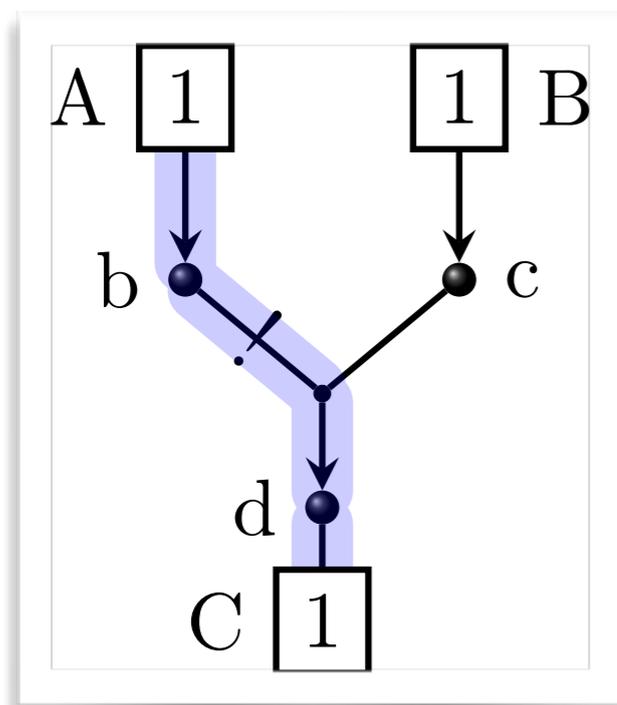


1 - avoid data loss when the **context** (FIFO) can receive the data.

2 reasons for context



2 - give **priority** based on the **context** (writer)

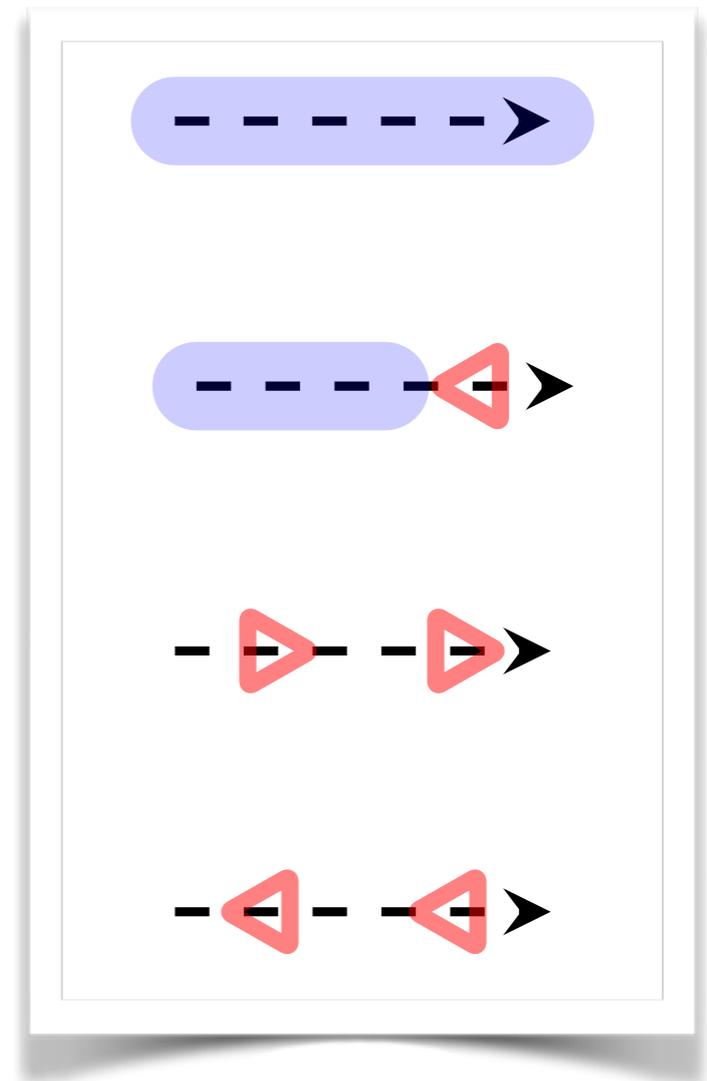
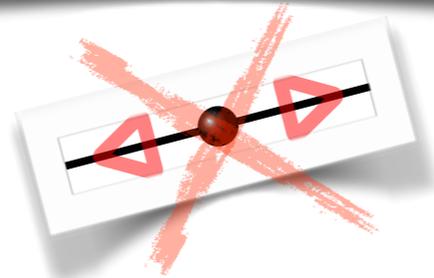
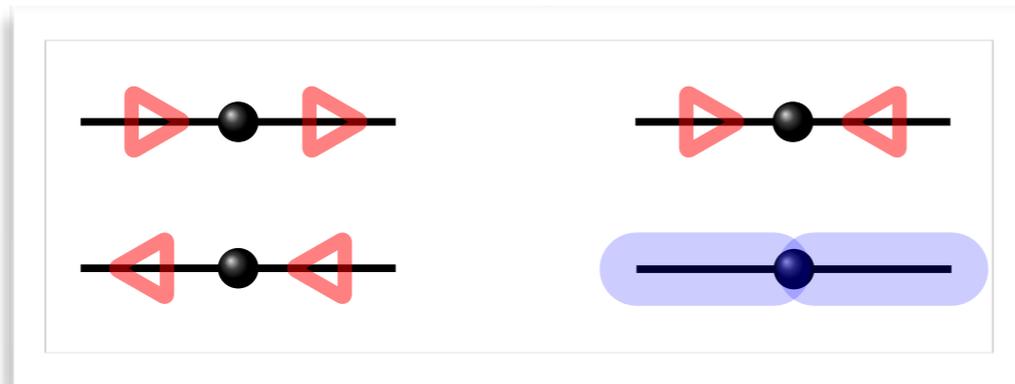


Context = 3 colours

- *Colouring*:

End \rightarrow {Flow, GiveReason, GetReason}

- *Composition* = matching colours:



Context = 3 colours

- *Context* End = $\{e_1, \dots, e_n\} \cup \{\bar{e}_1, \dots, \bar{e}_n\}$

End \rightarrow {Flow, GiveReason, GetReason}

- *Composition* = matching colours:

$$CT_1 \bowtie CT_2 =$$

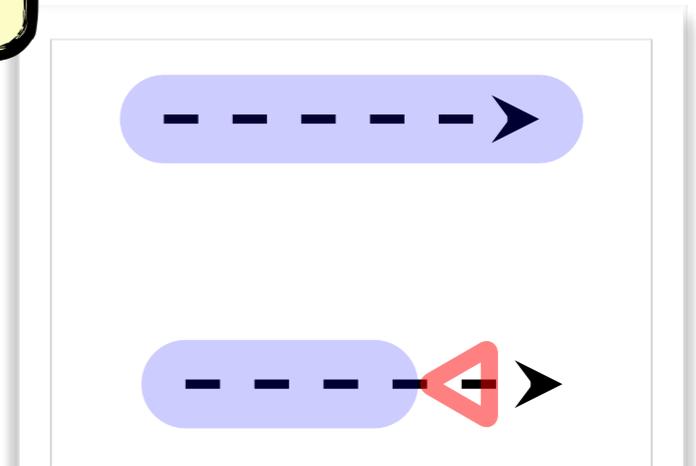
$$\{cl_1 \bowtie cl_2 \mid cl_1 \in CT_1, cl_2 \in CT_2, cl_1 \frown cl_2\}$$

$$cl_1 \frown cl_2 = \forall e_1 \in \text{dom}(cl_1) \cdot \forall e_2 \in \text{dom}(cl_2).$$

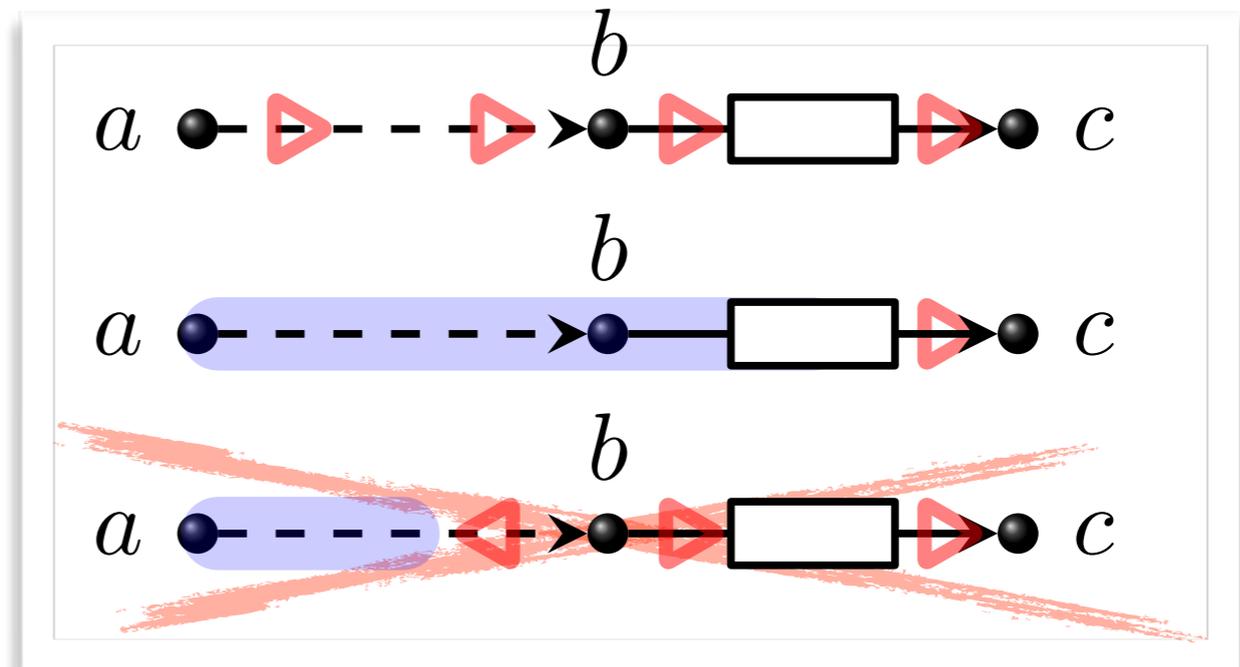
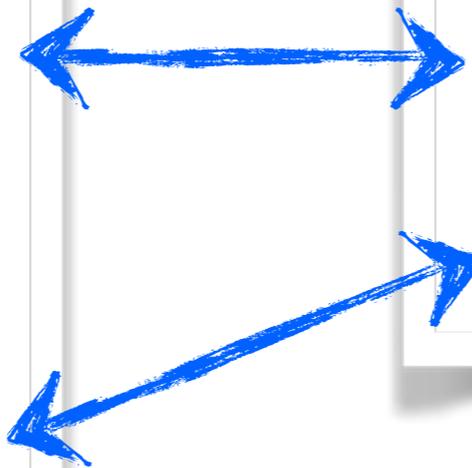
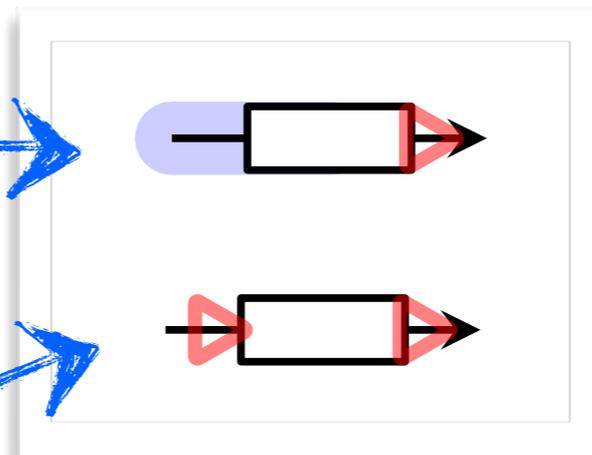
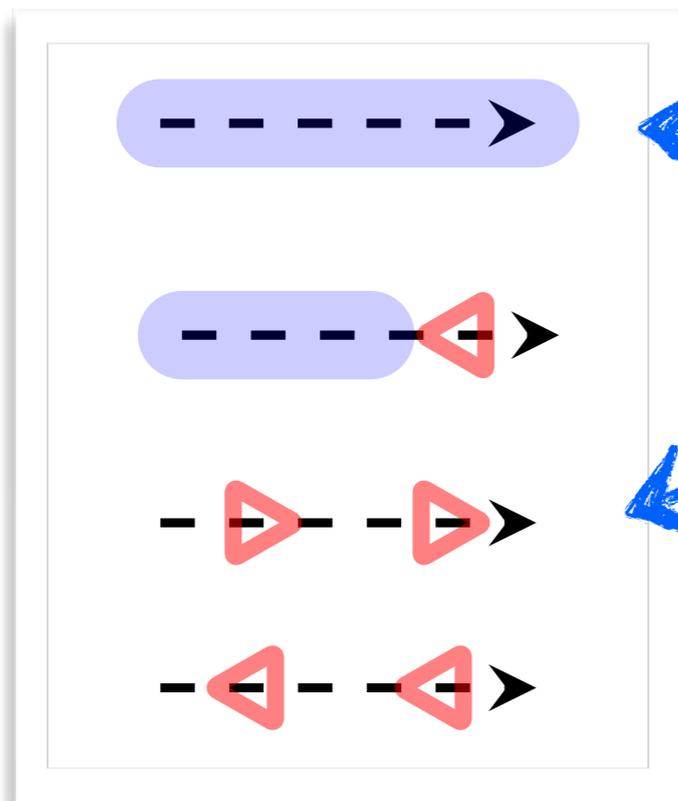
$$e_1 = \bar{e}_2 \Rightarrow$$

$$(cl_1(e), cl_2(e)) \in \{(\blacktriangleright, \blacktriangleright), (\blacktriangleleft, \blacktriangleleft), (\blacktriangleright, \blacktriangleleft), \}$$

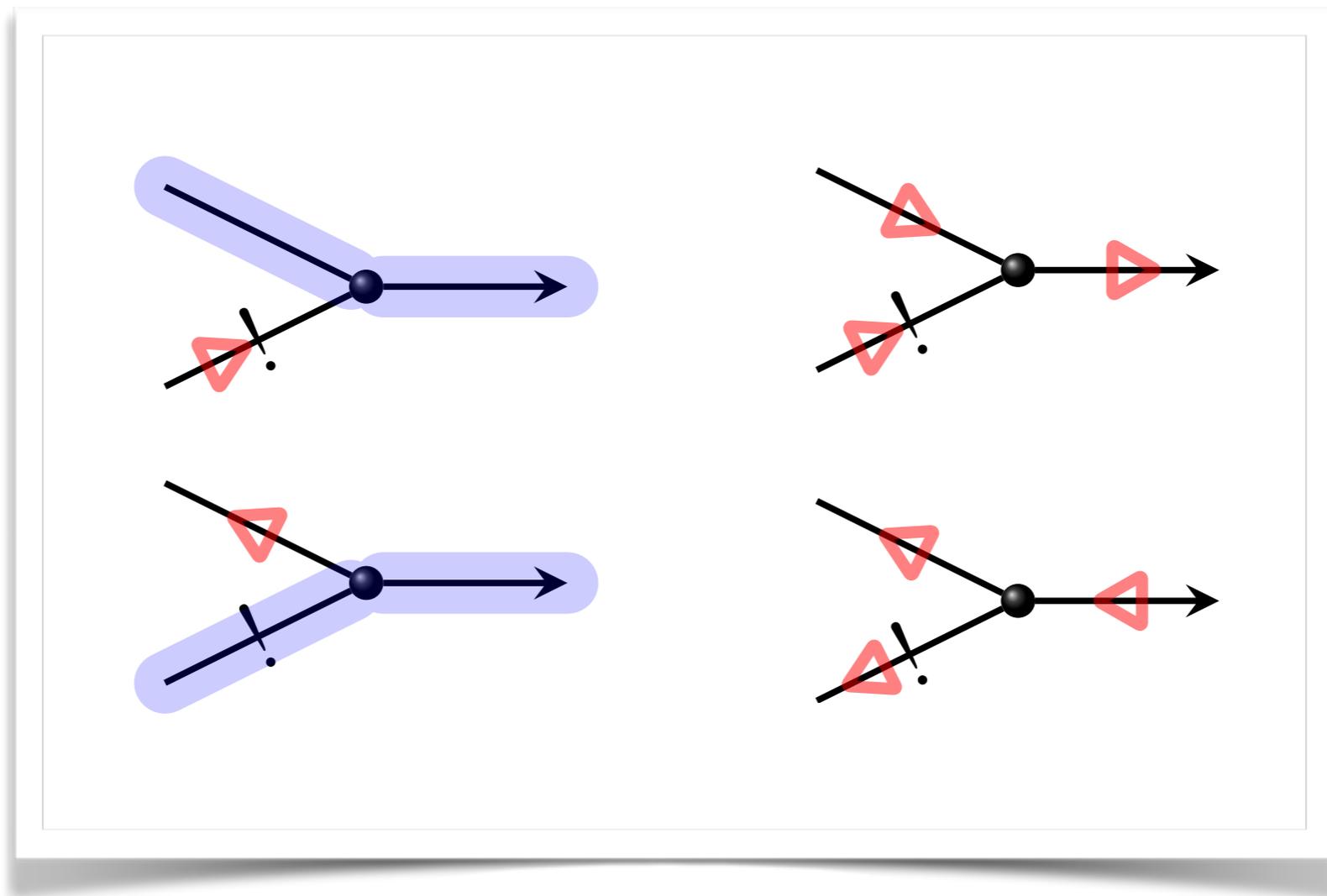
$$cl_1 \bowtie cl_2 = cl_1 \cup cl_2$$



Composition



Priority with 3 colours



Connector colouring 3

- **Compositional** – composition operation is associative, commutative, and does not require post-processing.
- *Reasons* for the absence of flow are **propagated**.
- Expresses **priority**.
- 2 colours \Leftrightarrow constraint automata (without data)
- 3 colours: + expressive (\Leftrightarrow intentional automata)

Build a connector

